

Tail Inequalities for Sums

- Possible to derive even stronger bounds on tail probabilities for the sum of independent *Bernoulli trials*
- <u>Chernoff Bound</u>: Let X1, ..., Xm be independent Bernoulli trials such that Pr[Xi=1] = p (Pr[Xi=0] = 1-p). Let $X = \sum_{i} X_{i}$ and $\mu = mp$ be the expectation of X. Then, for any $\varepsilon > 0$,

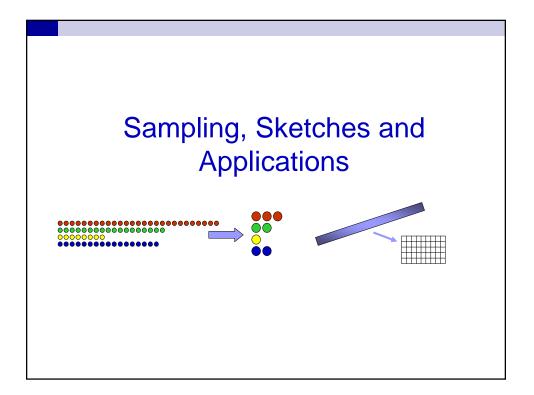
$$\Pr(|X-\mu| \ge \mu \epsilon) \le 2\exp^{\frac{-\mu \epsilon}{2}}$$

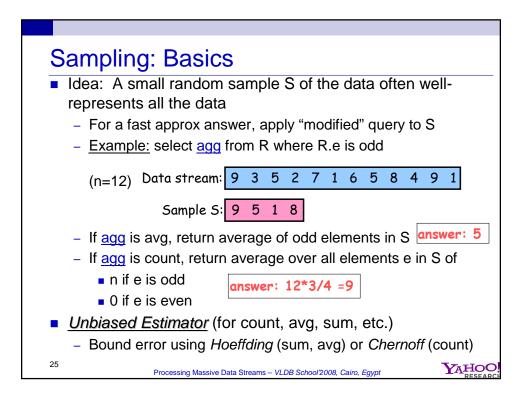
- Application: Sample selectivity ≈ population selectivity
 See below...
- Remark: Chernoff bound results in tighter bounds for count queries compared to Hoeffding bound

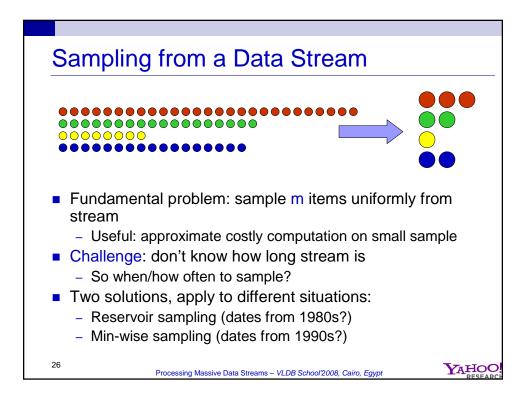


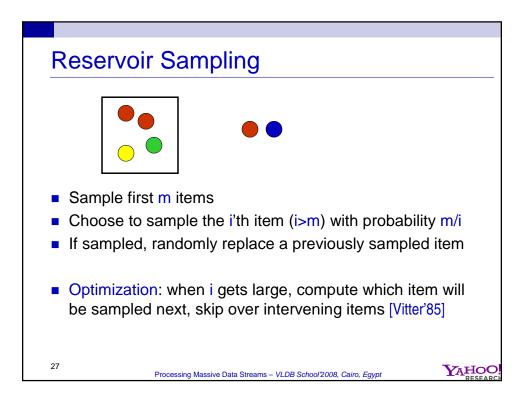
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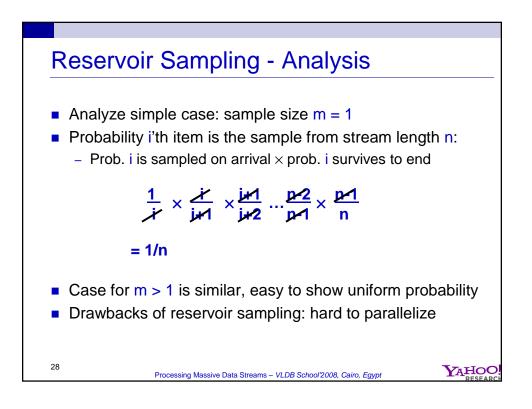
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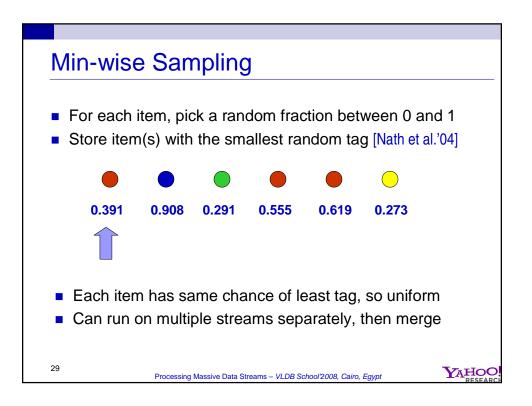


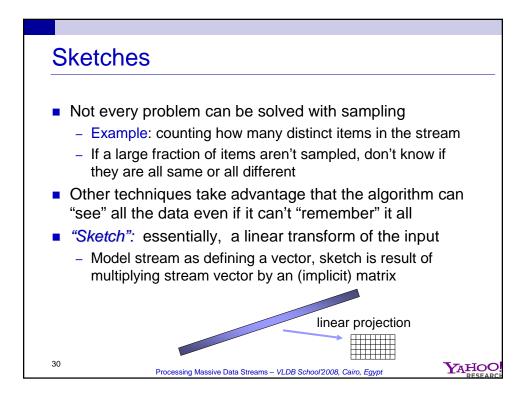


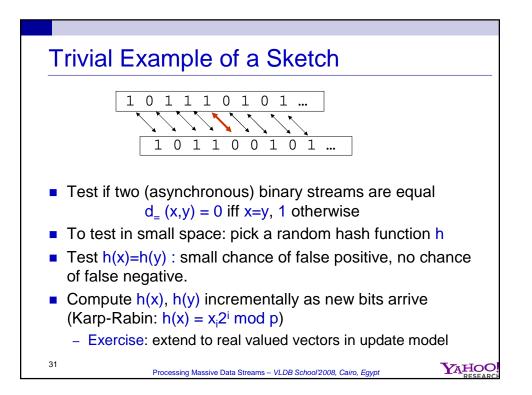


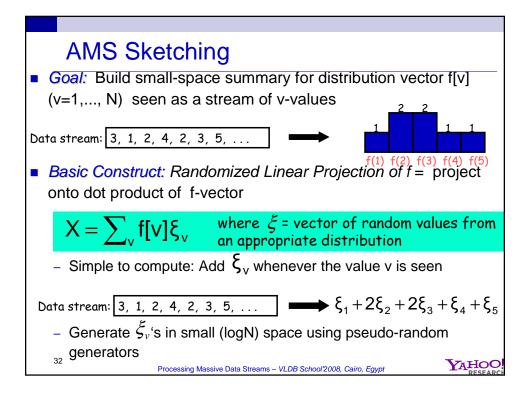


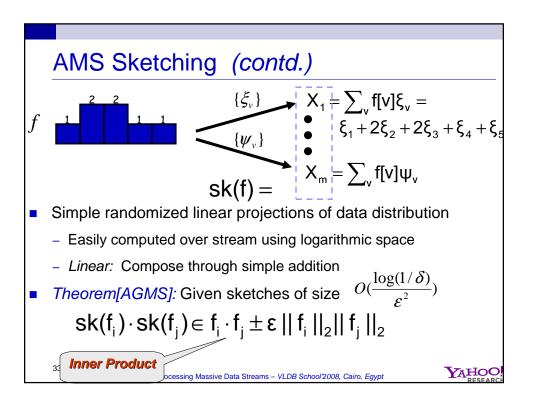


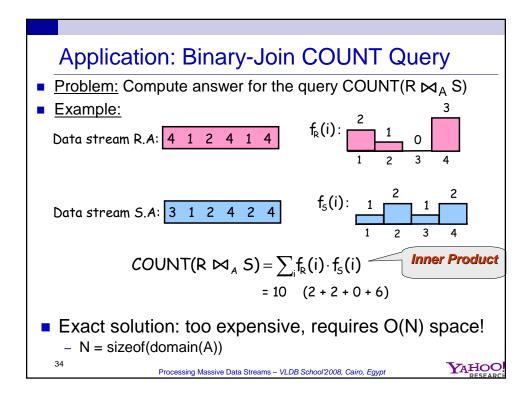


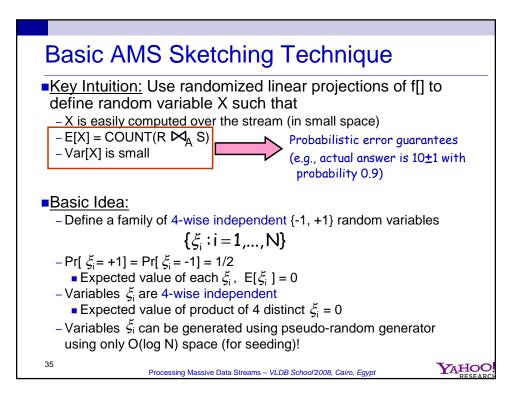


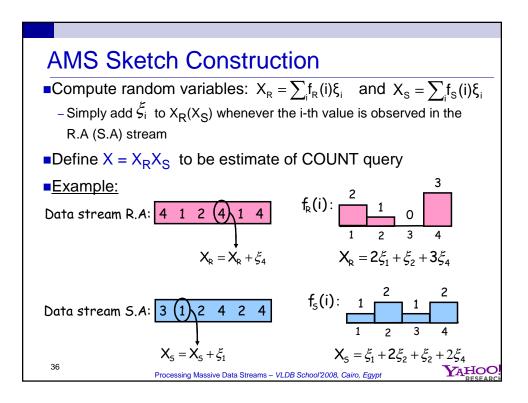


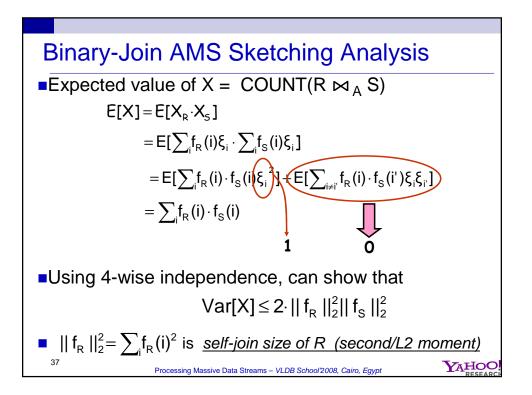


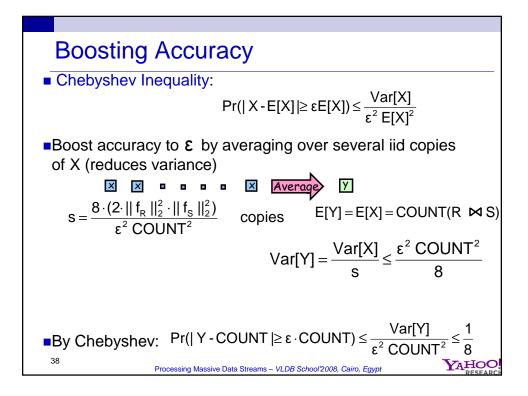


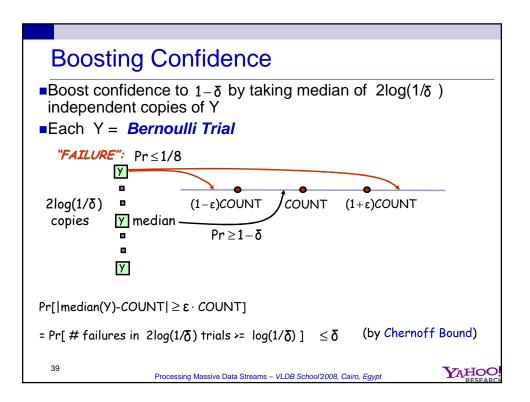


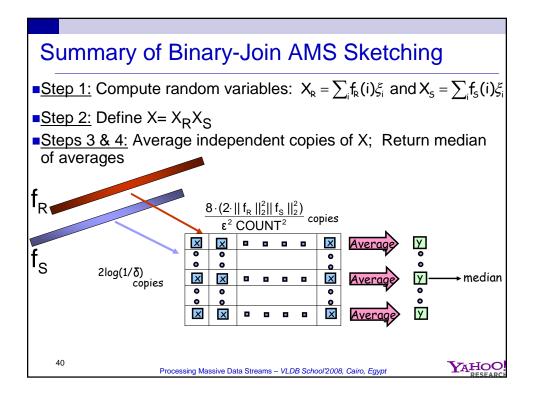


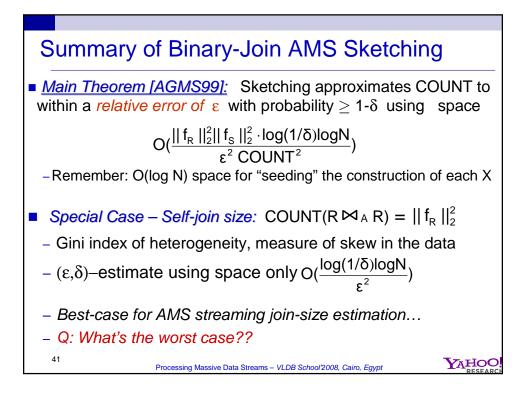


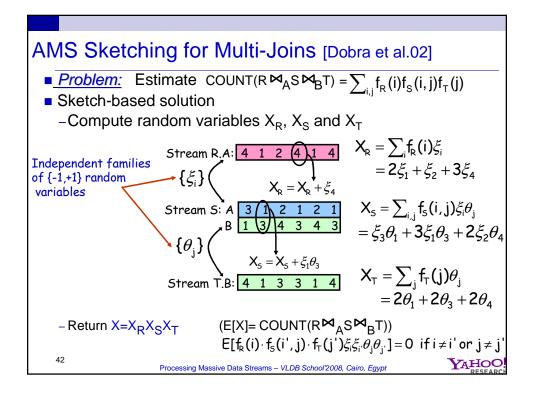


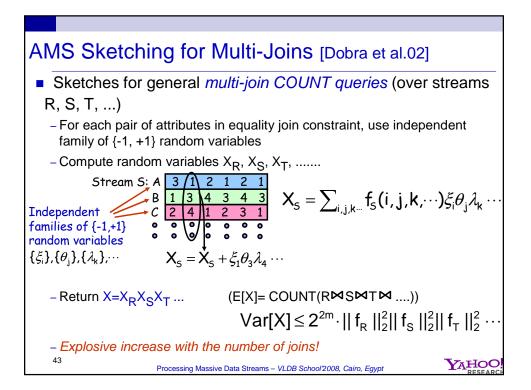


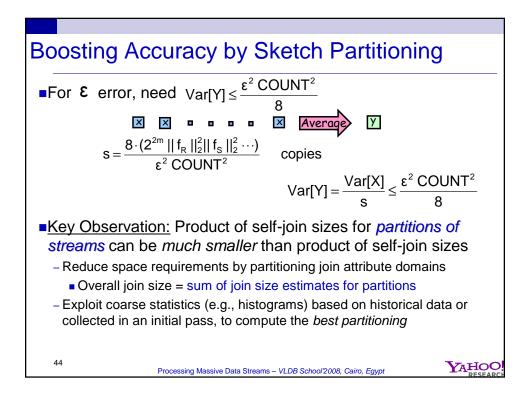


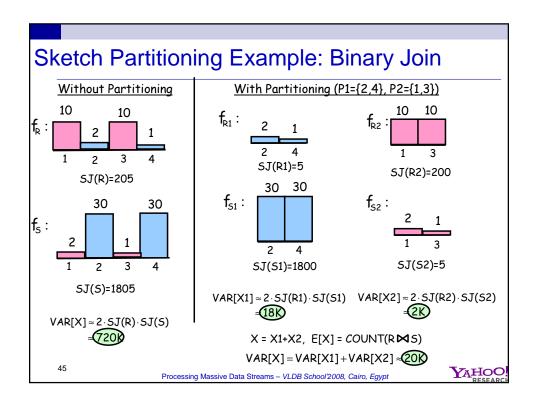


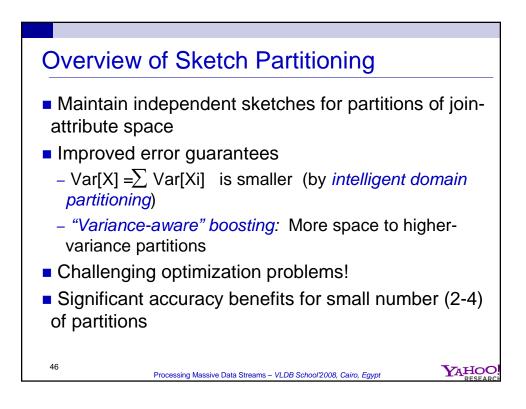


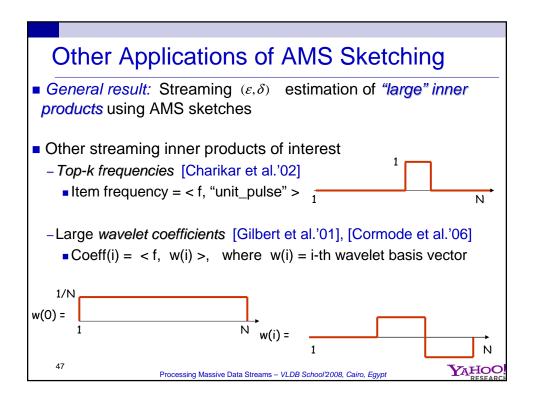


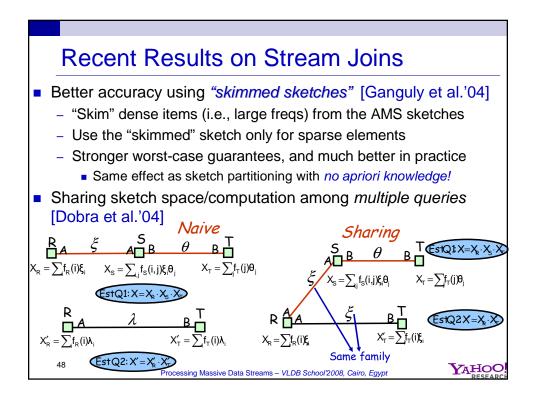


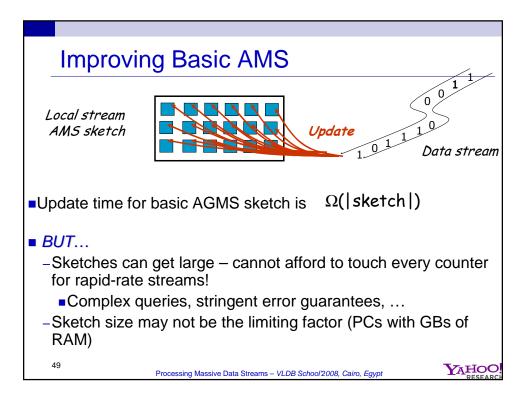


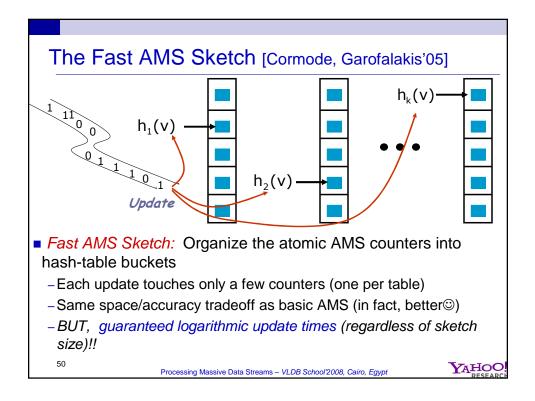


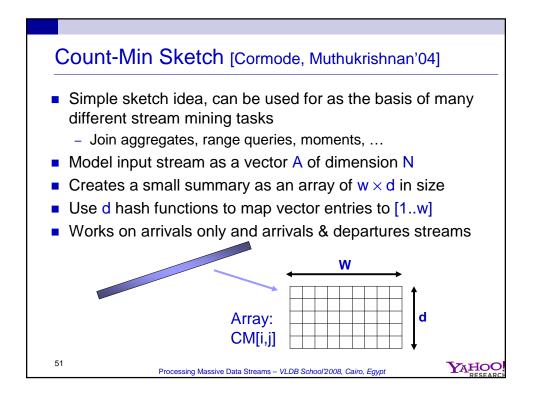


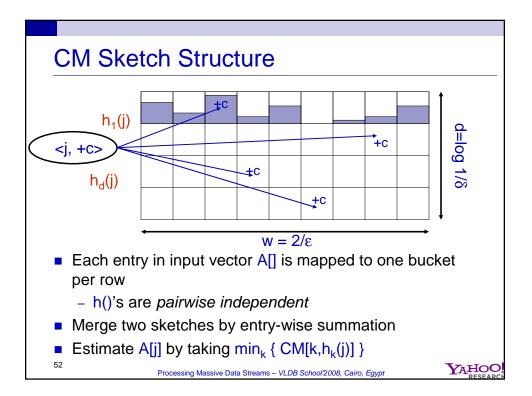


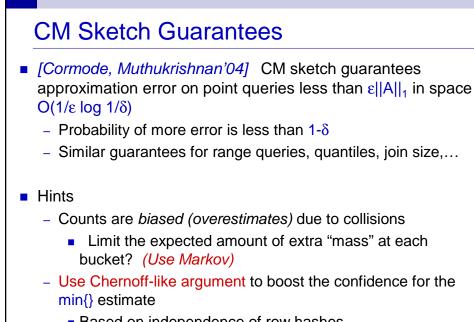






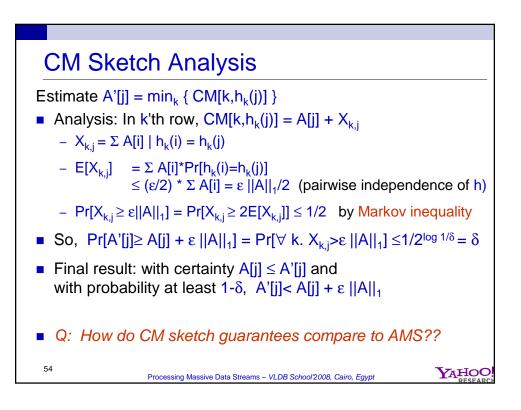


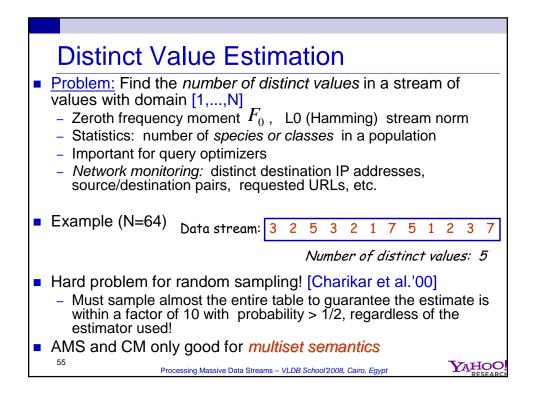


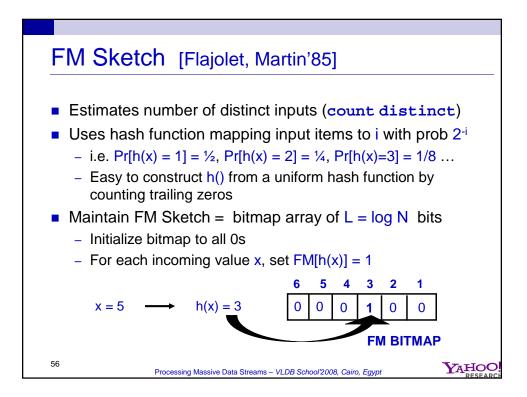


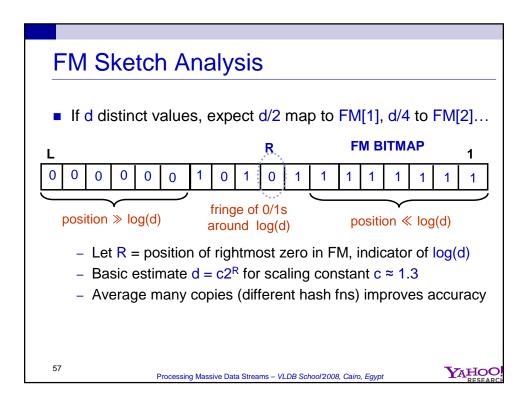


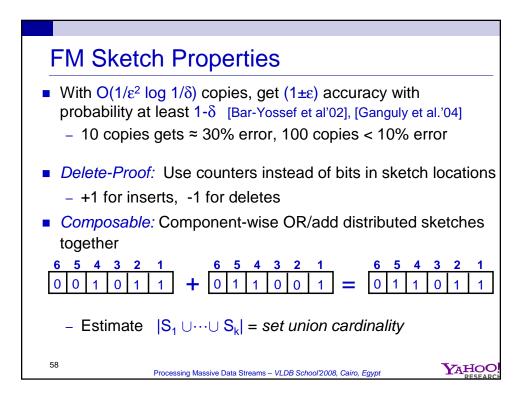
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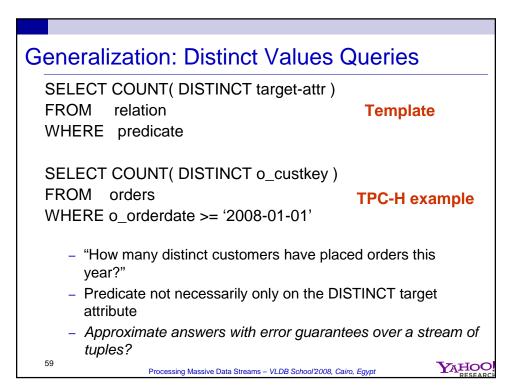


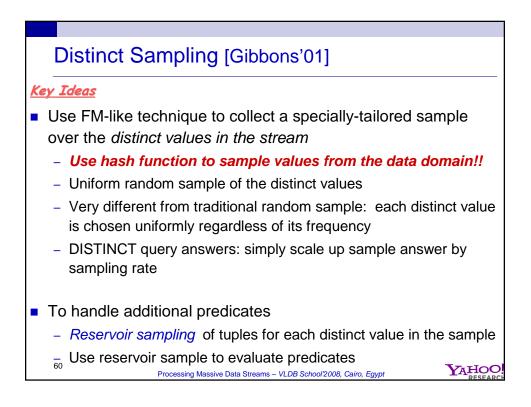


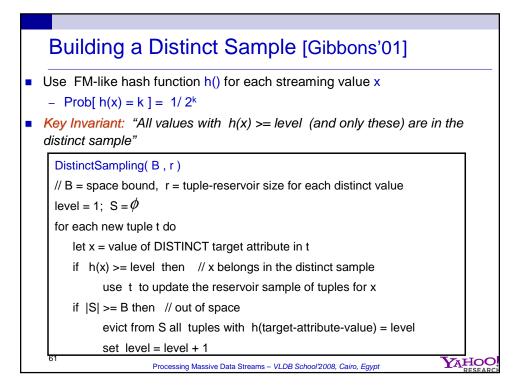


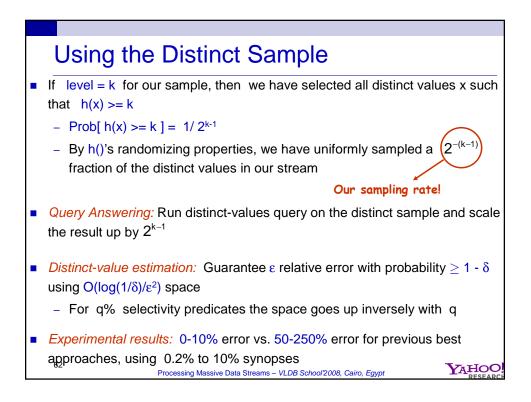


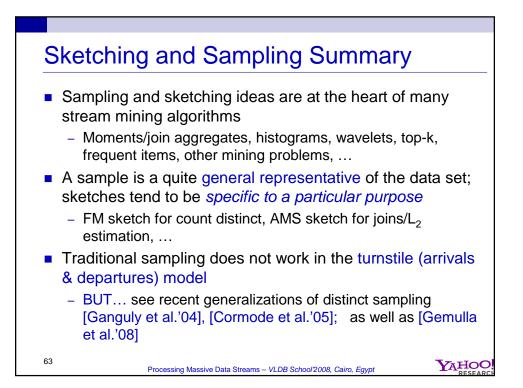


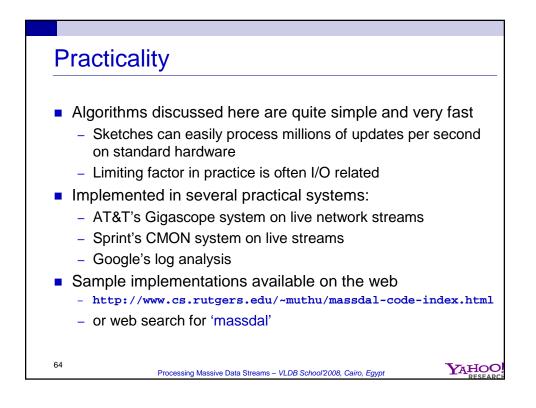


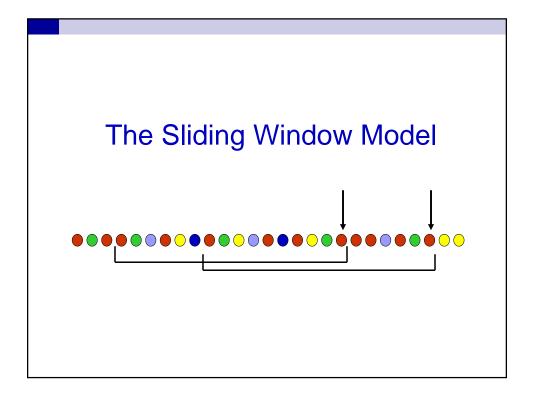


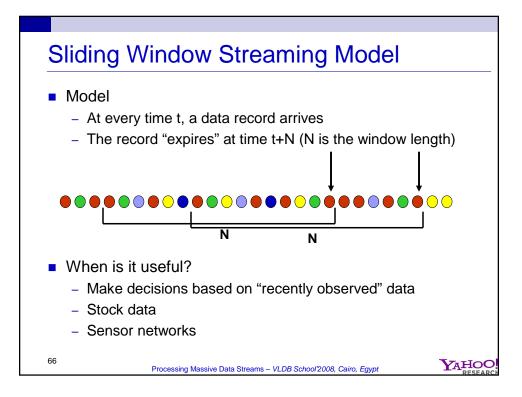


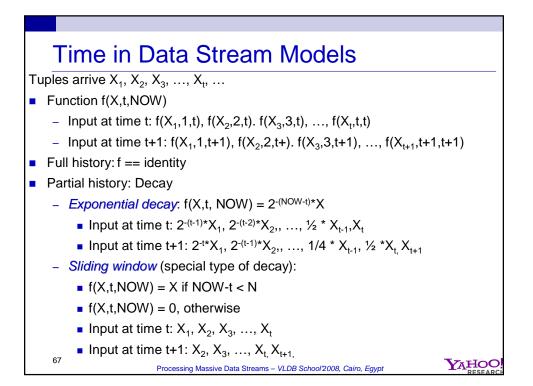


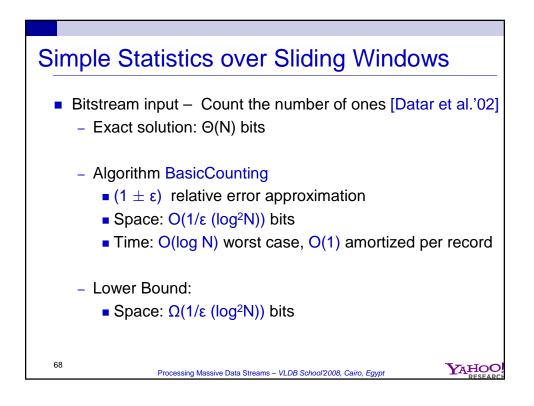


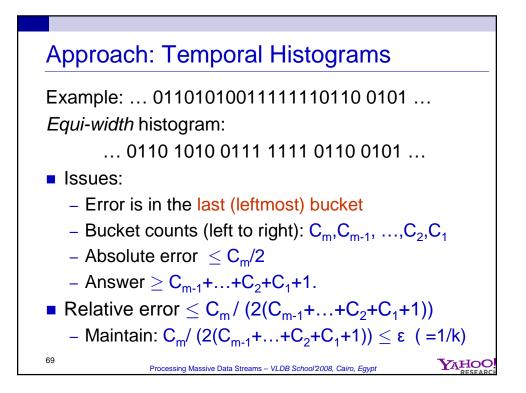


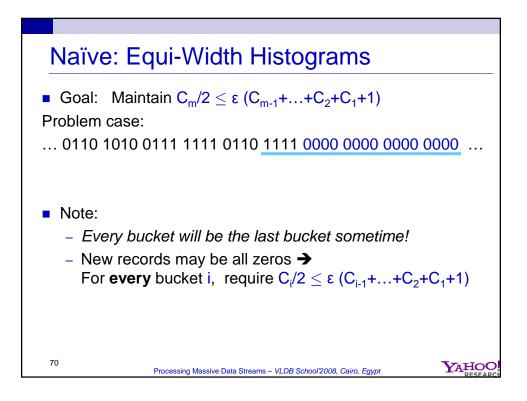


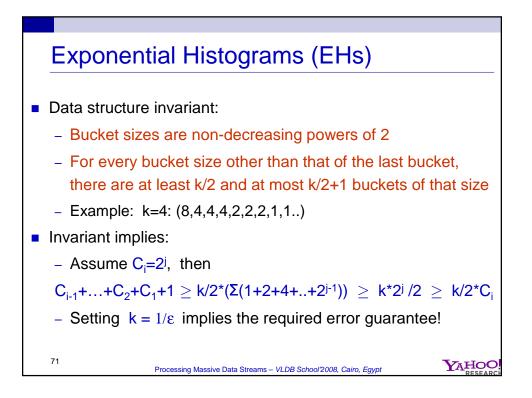


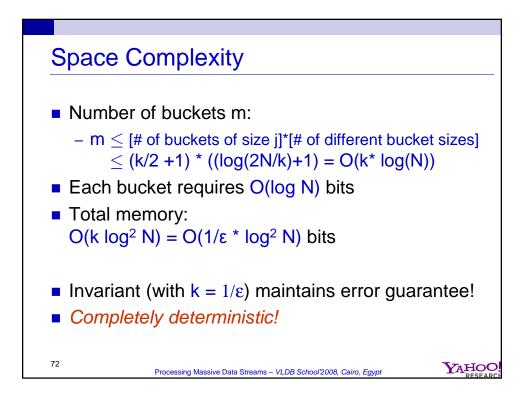


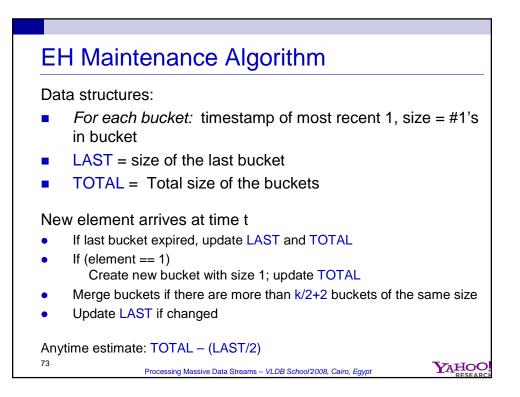


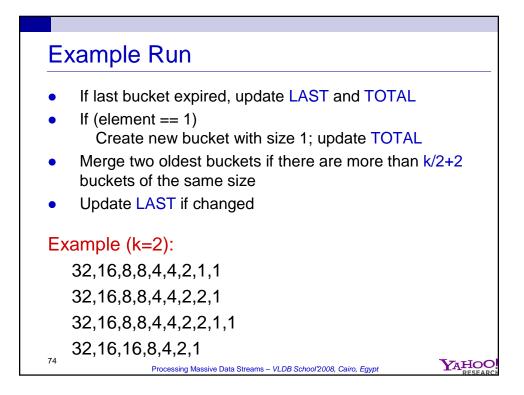


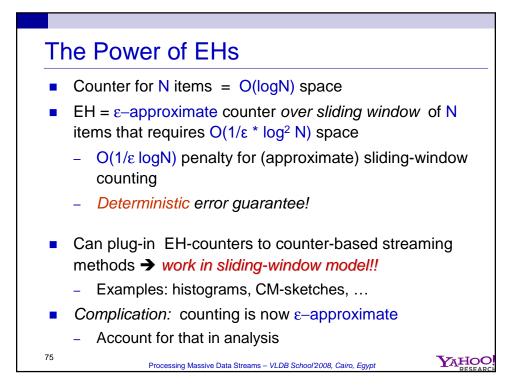


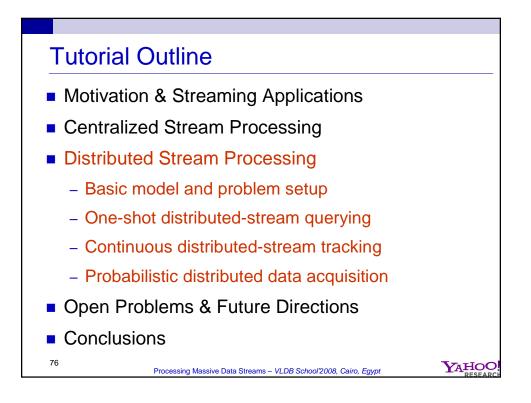


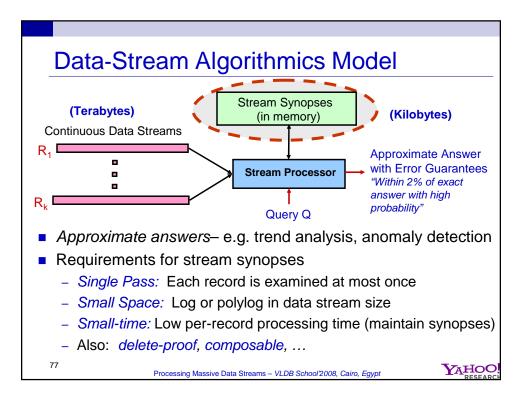


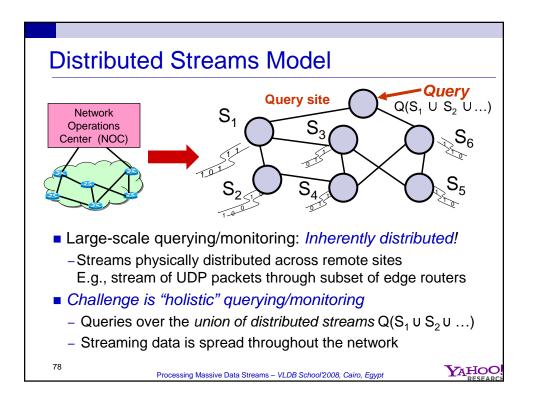


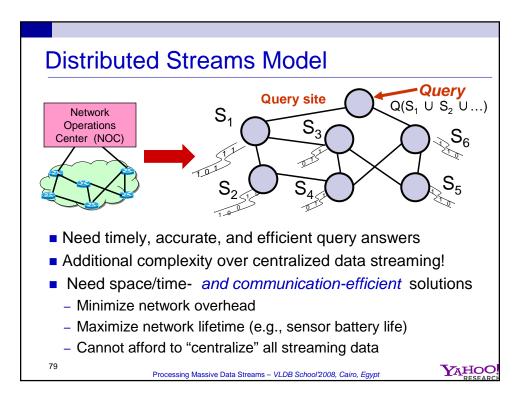


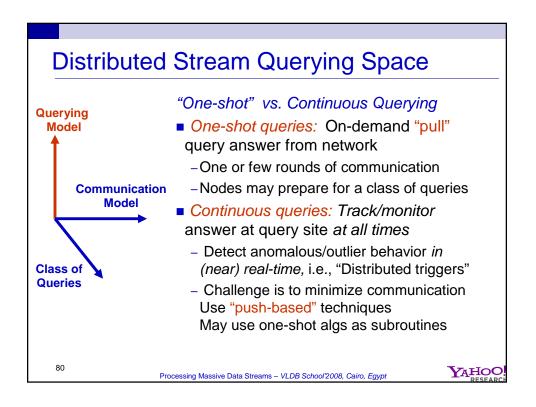




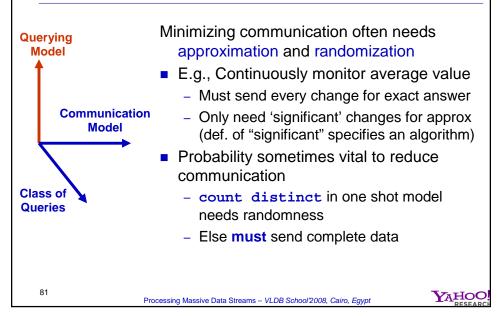


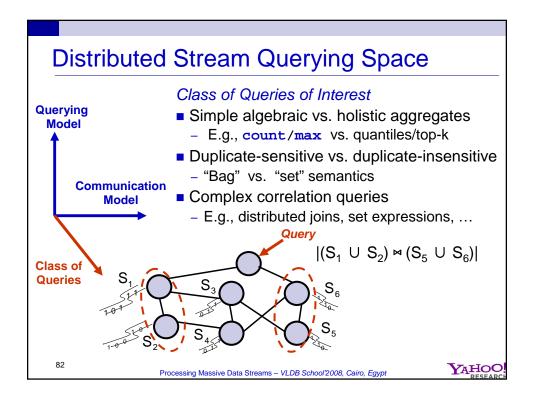


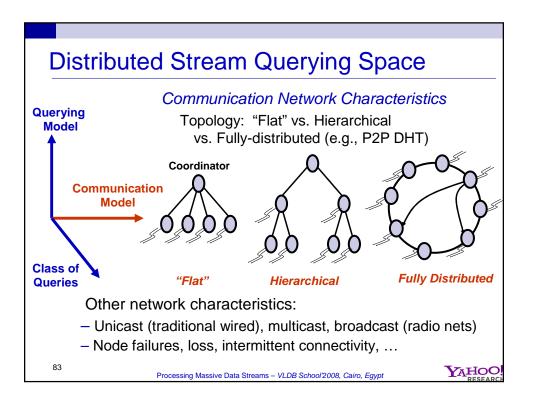


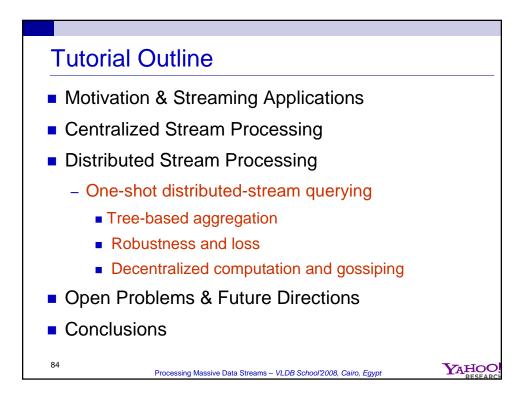


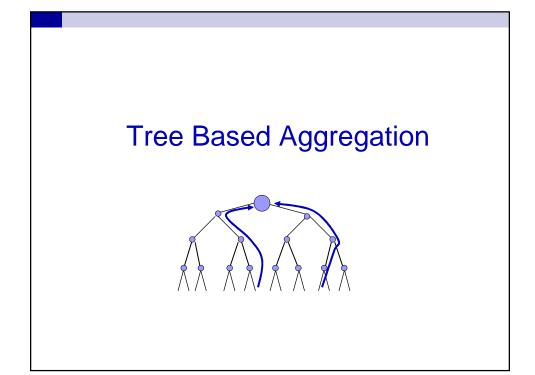
Distributed Stream Querying Space

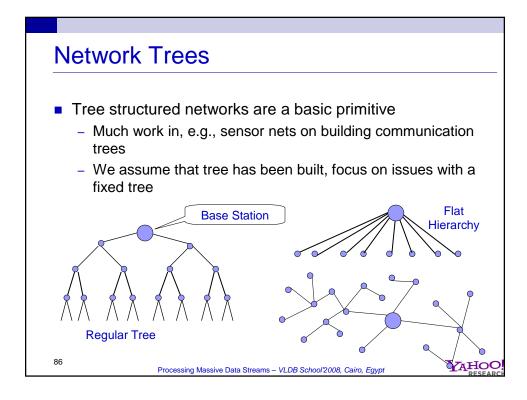


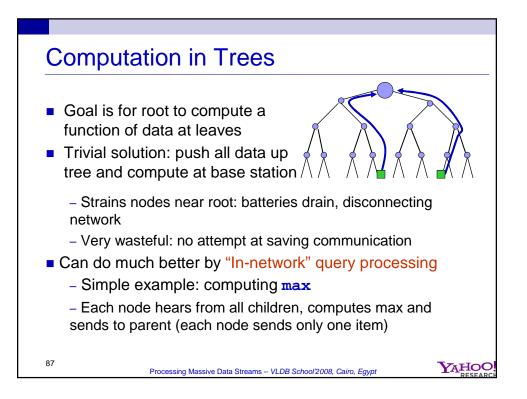


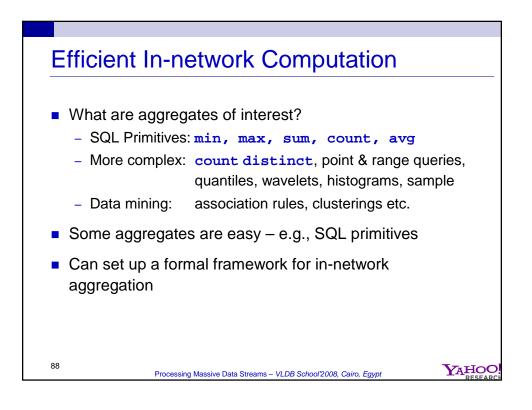


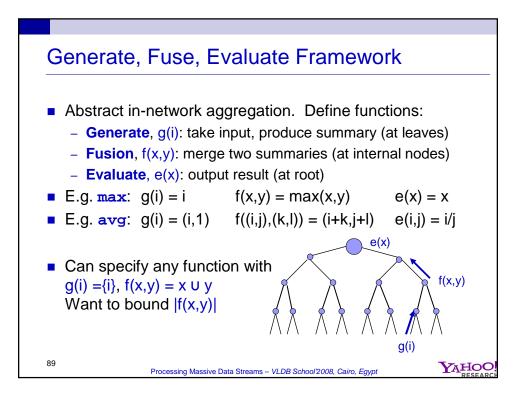


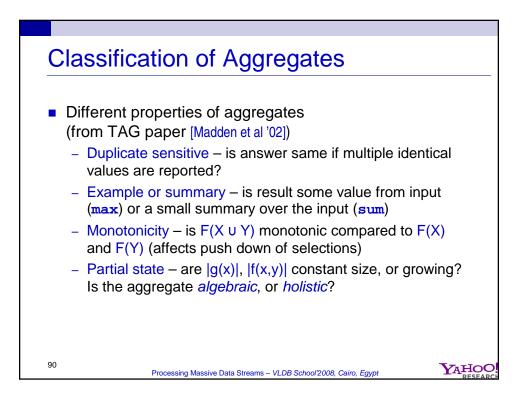




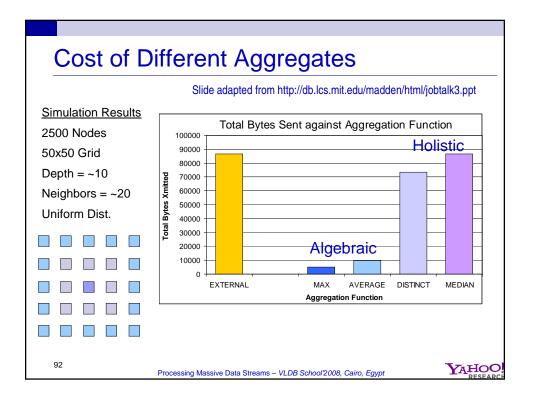


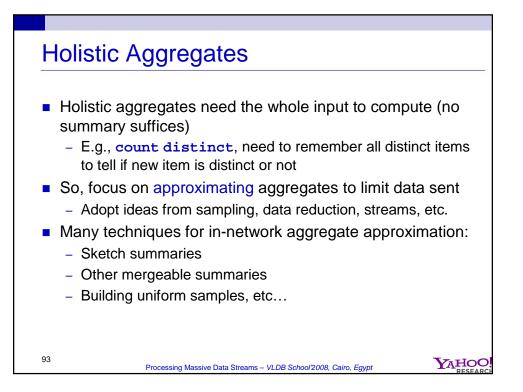


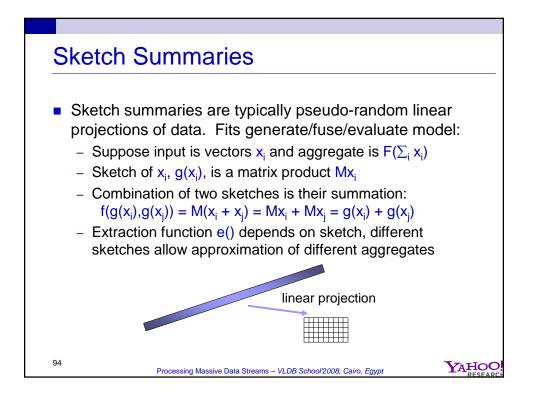


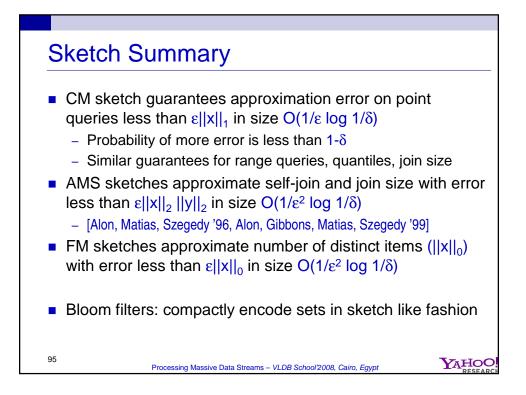


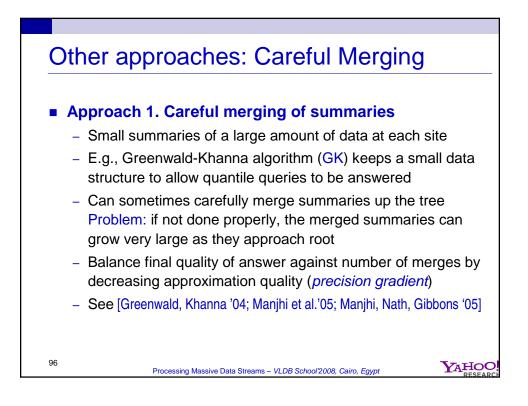
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sum, count	Yes	Summary	Yes	algebraic
average	Yes	Summary	No	algebraic
median, quantiles	Yes	Example	No	holistic
count distinct	No	Summary	Yes	holistic
sample	Yes	Example(s)	No	algebraic?
histogram	Yes	Summary	No	holistic

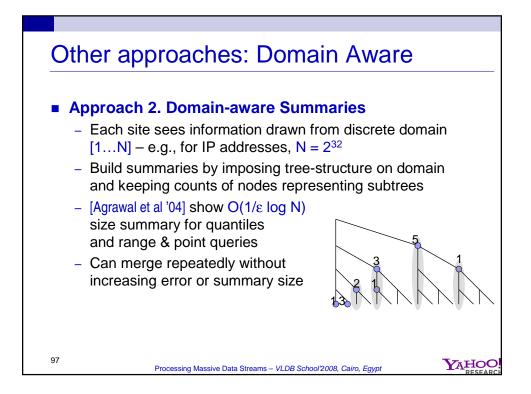


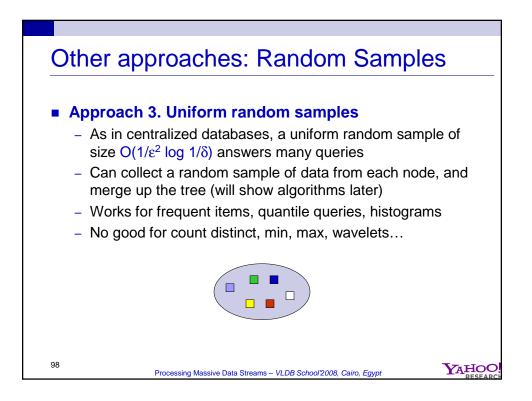


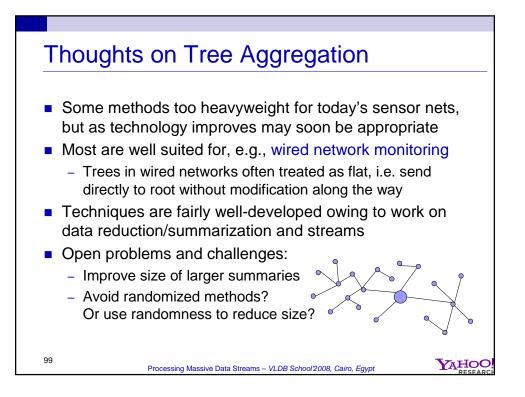


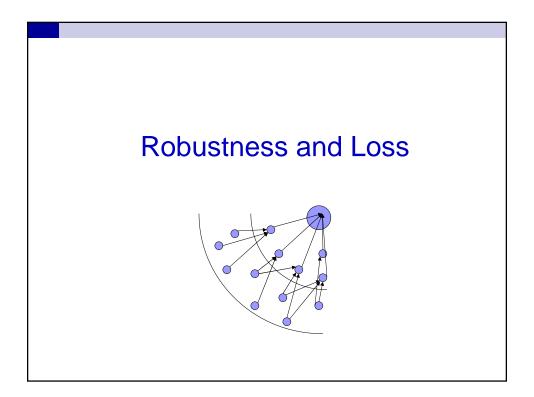


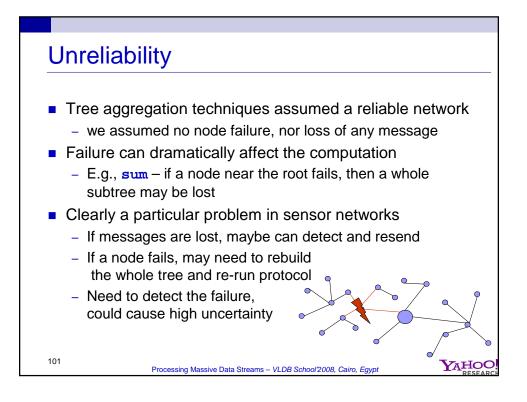


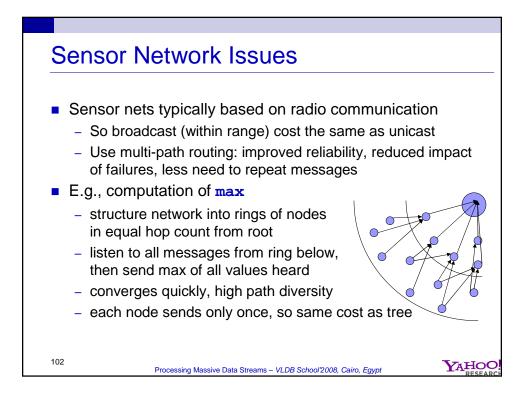


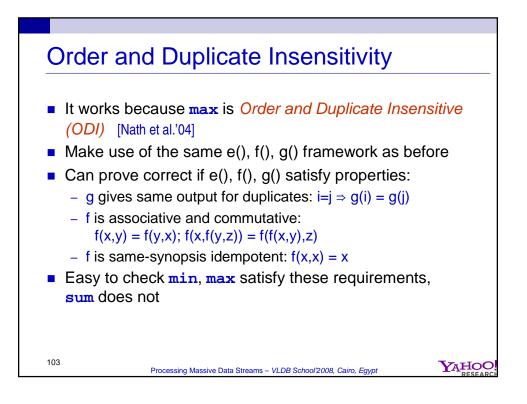


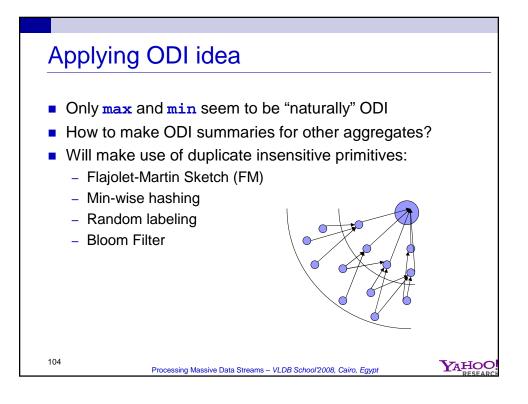


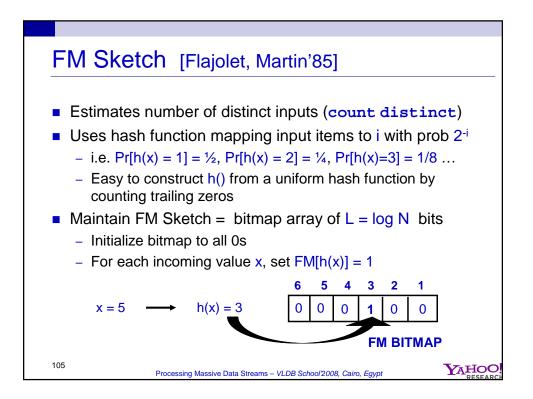


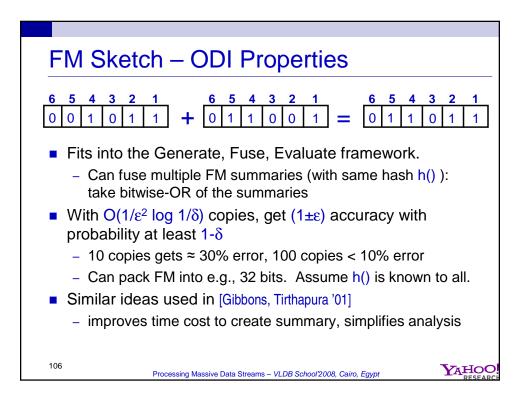


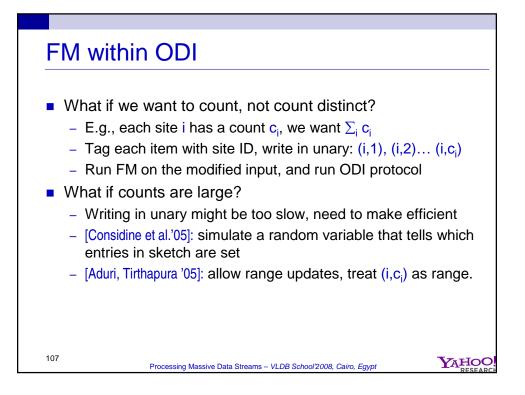


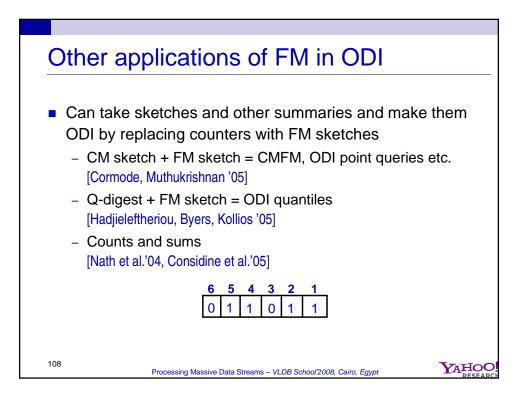


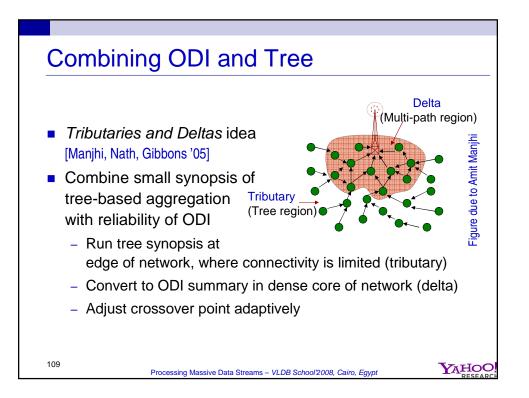


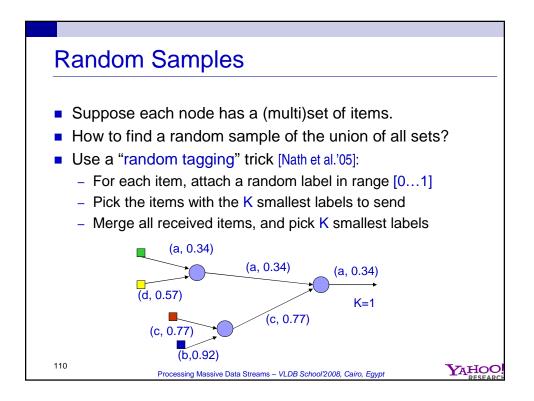


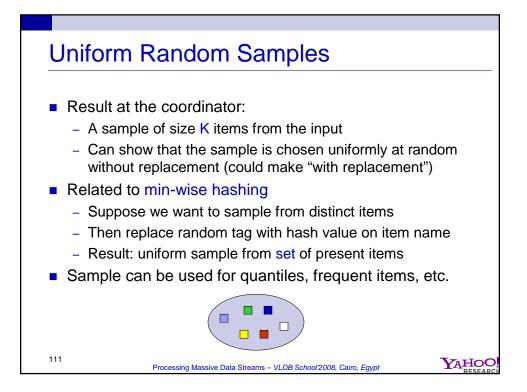


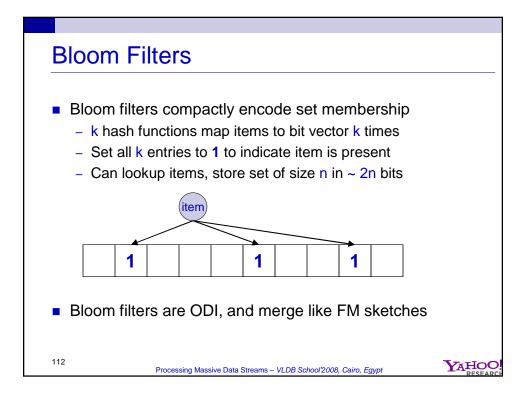


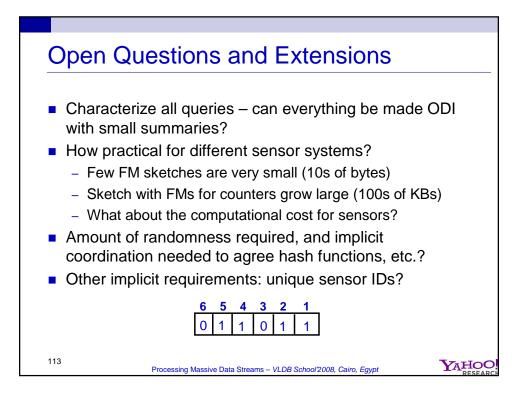


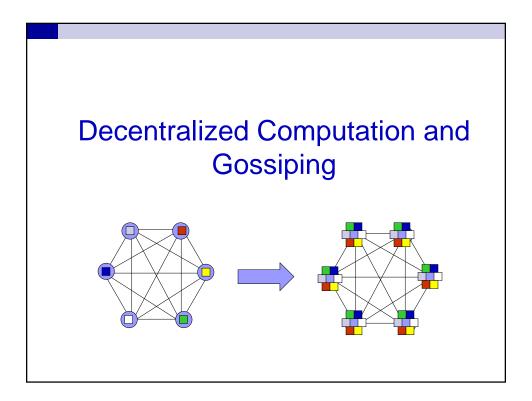


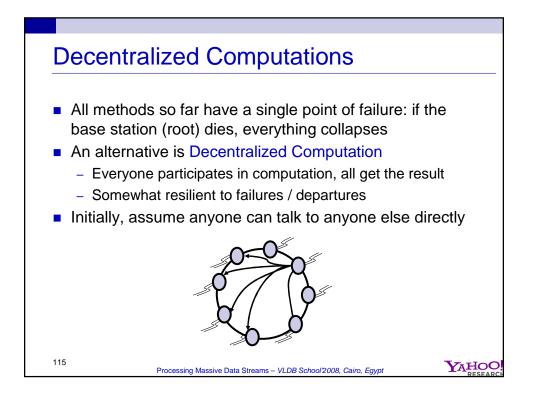


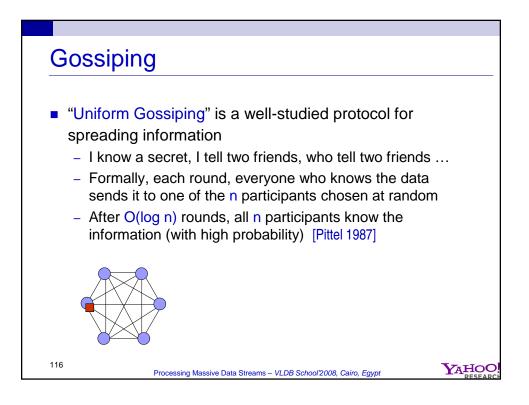


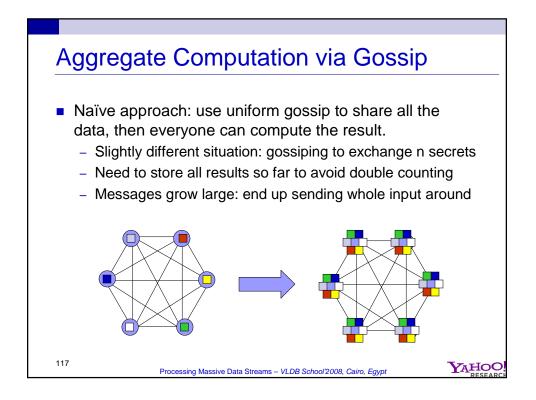


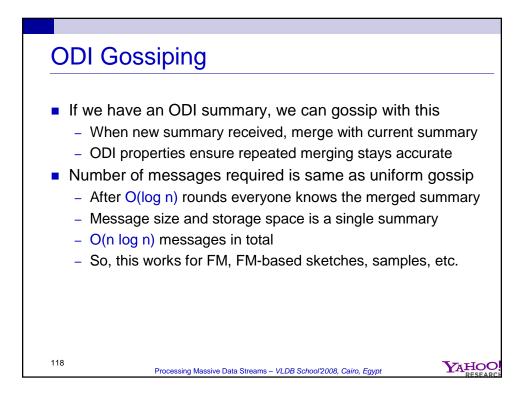


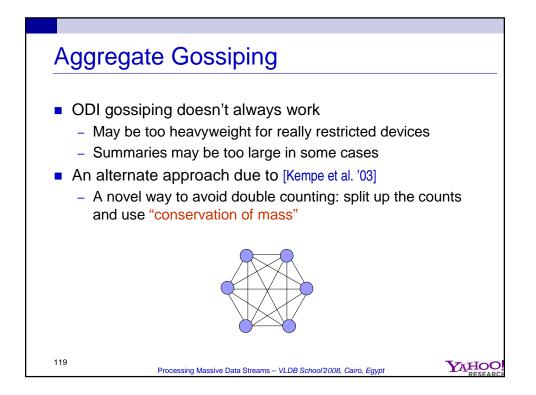


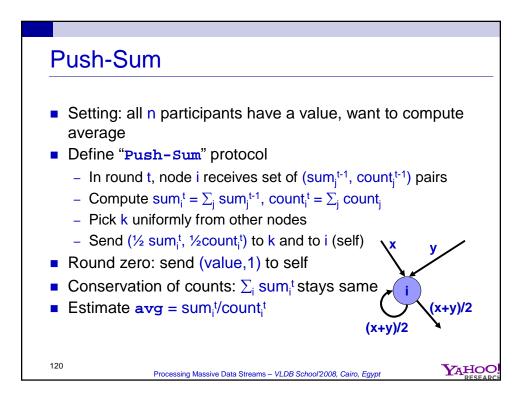


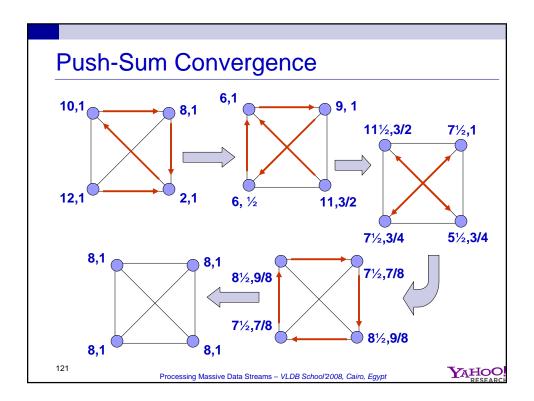


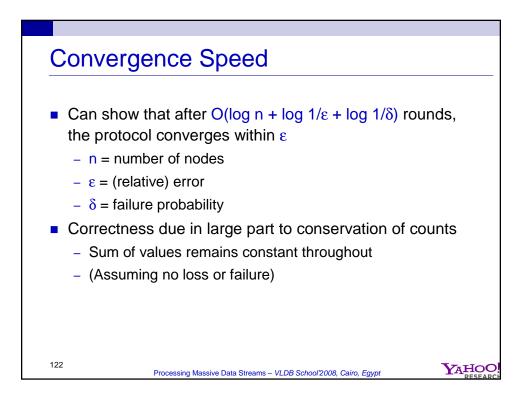


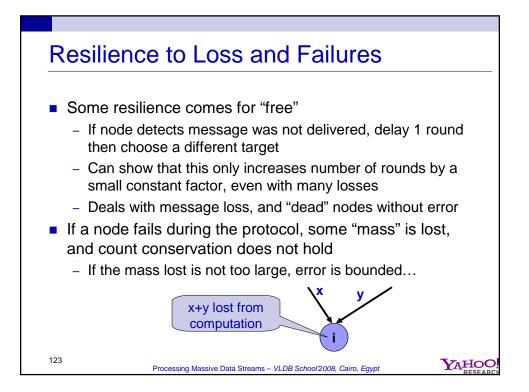


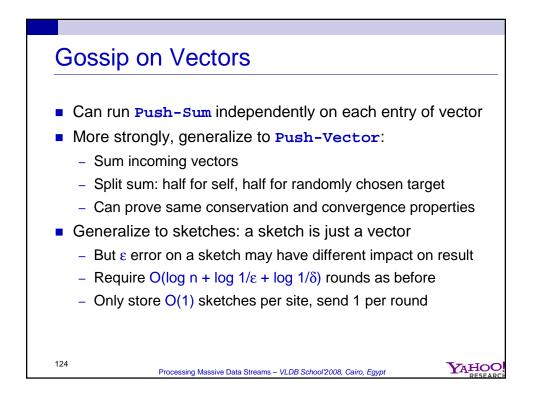


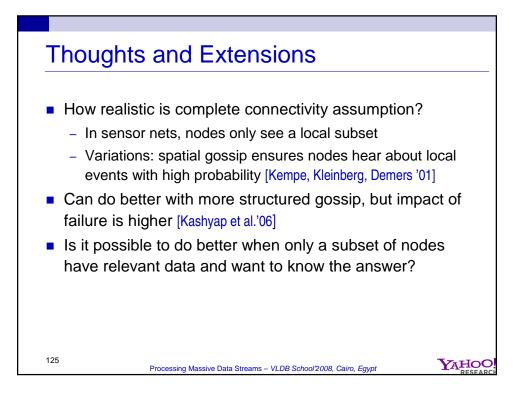


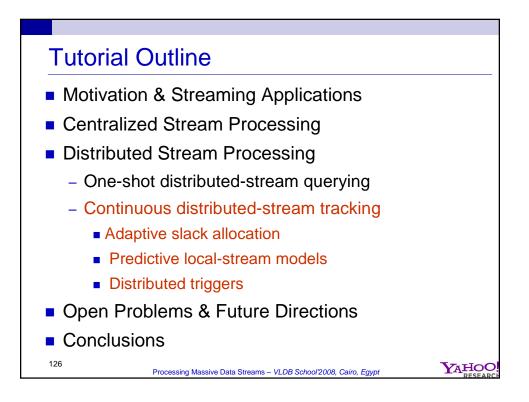


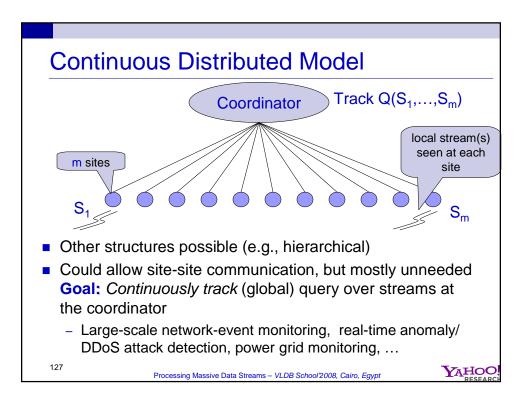


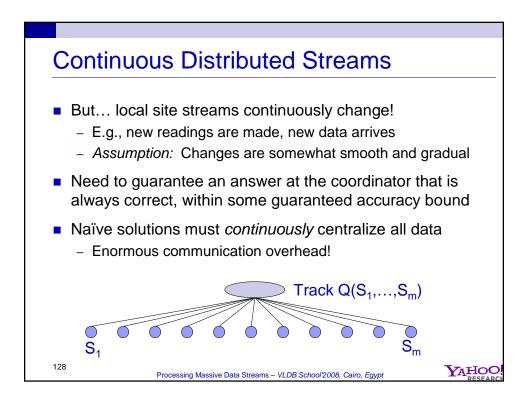


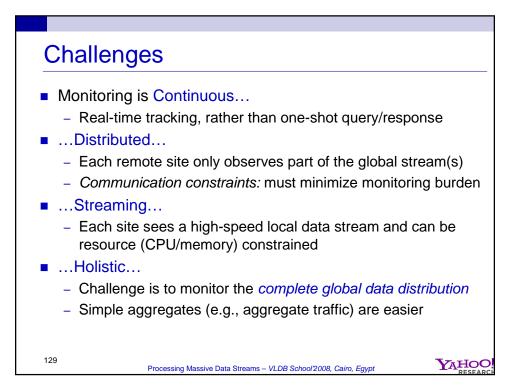


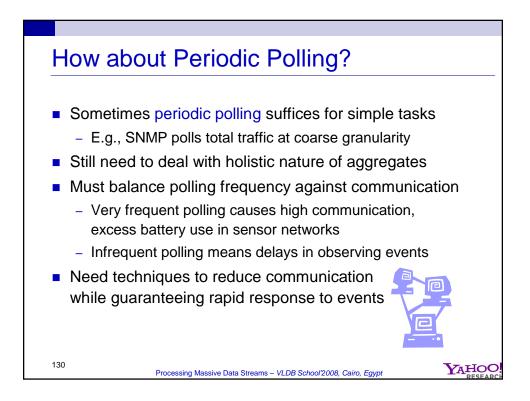


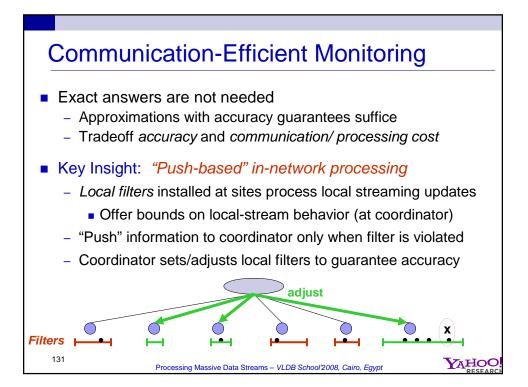


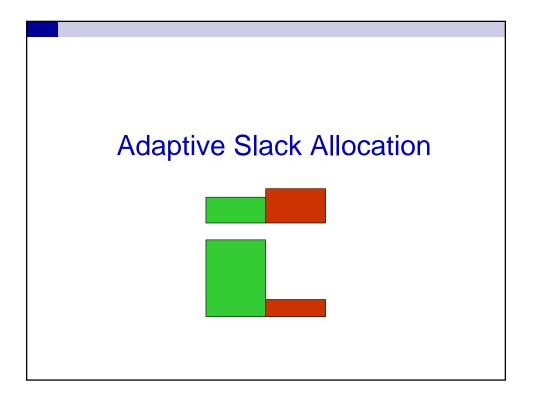


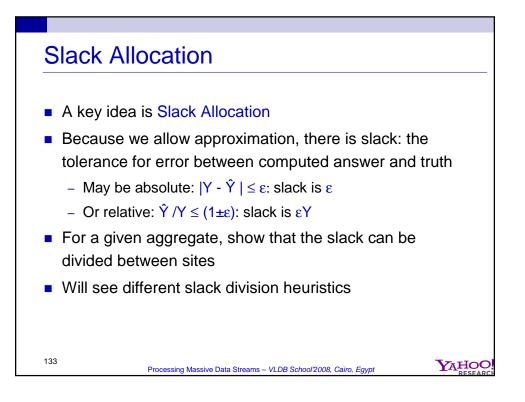


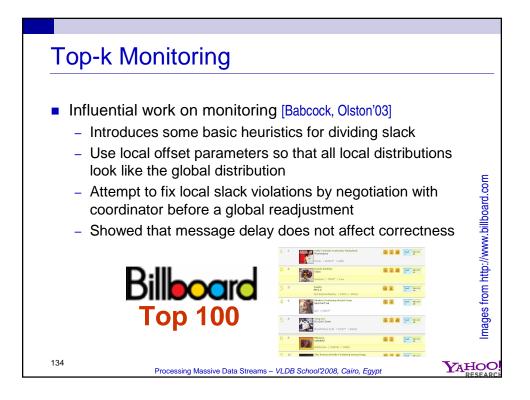


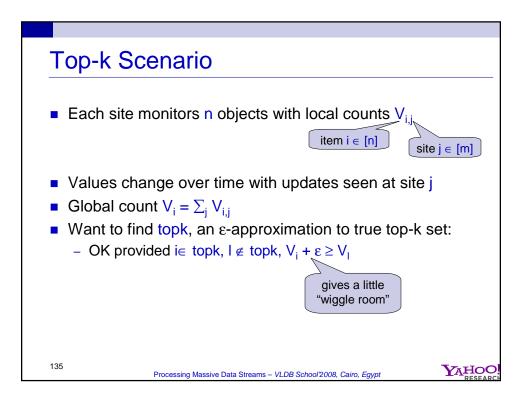


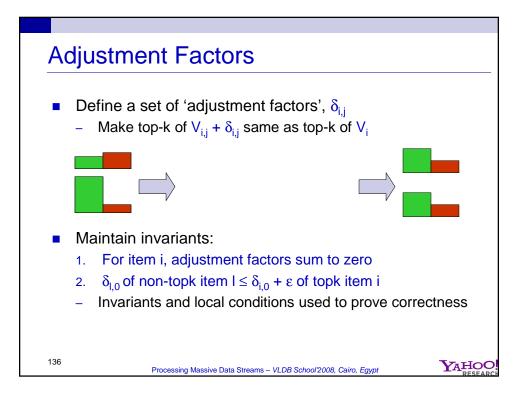


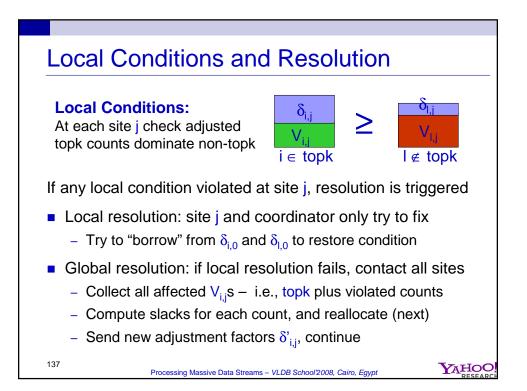


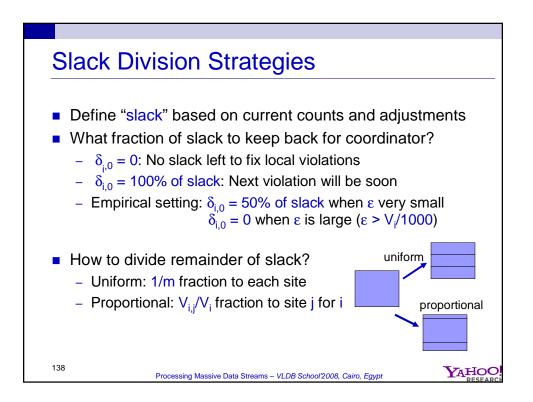




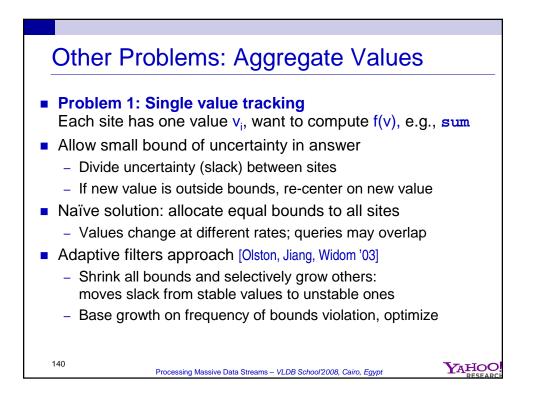


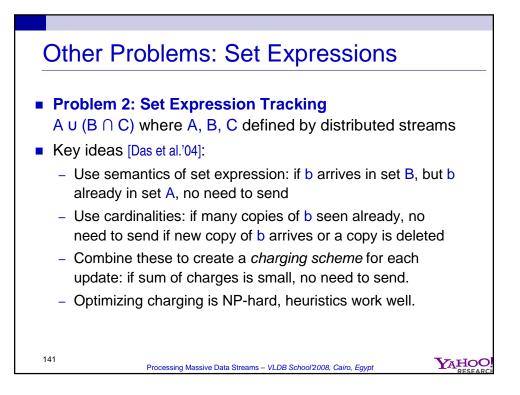


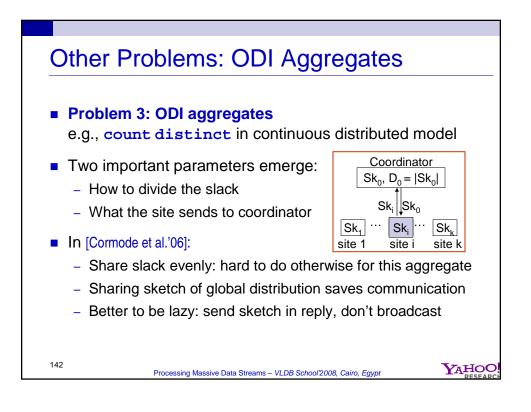


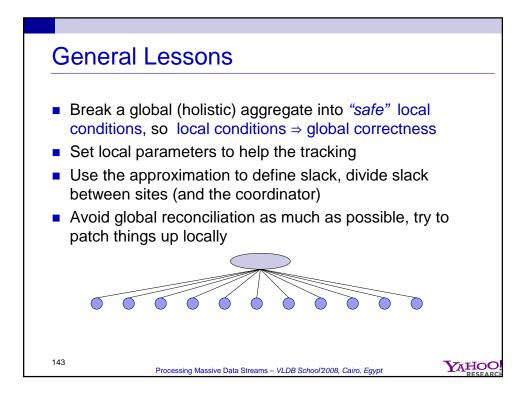


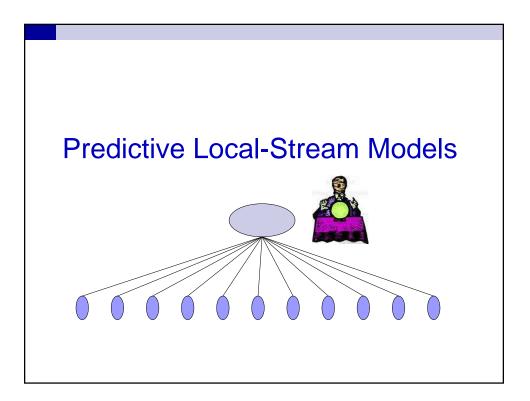


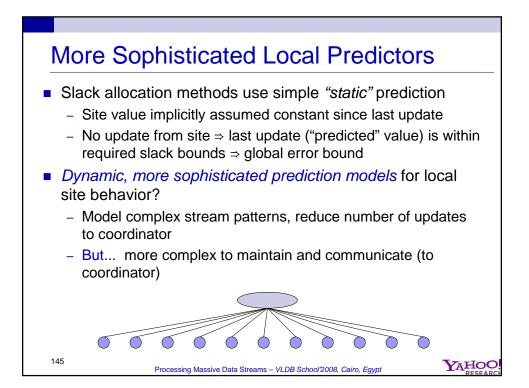


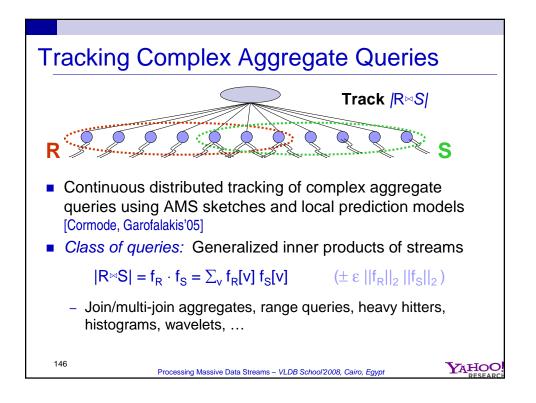


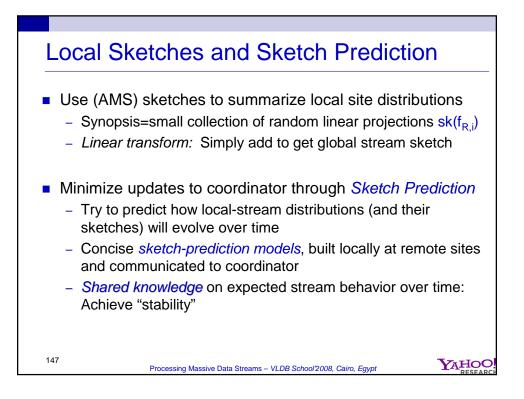


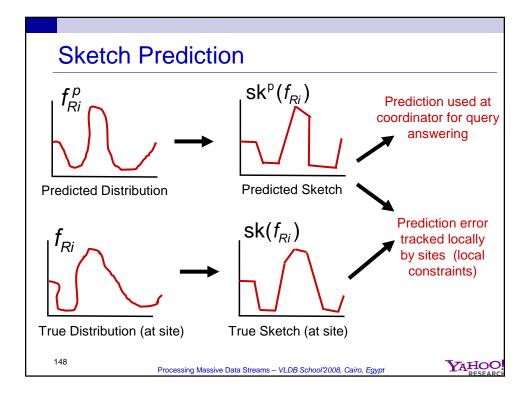


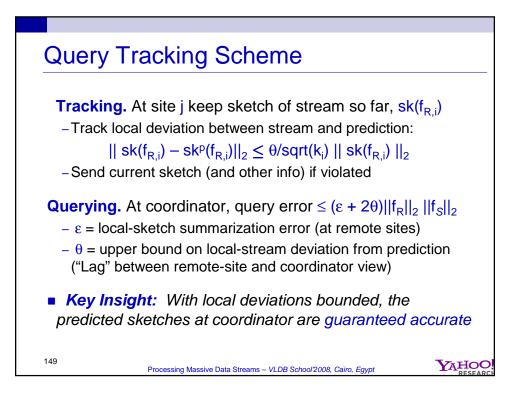


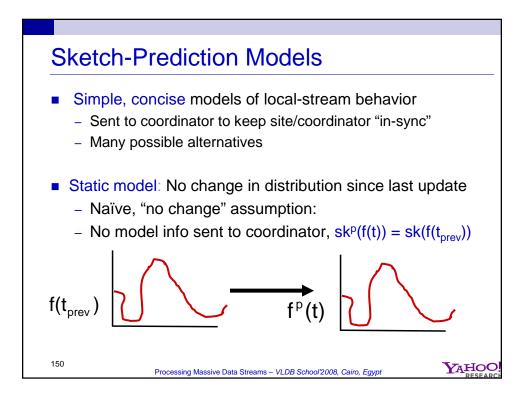


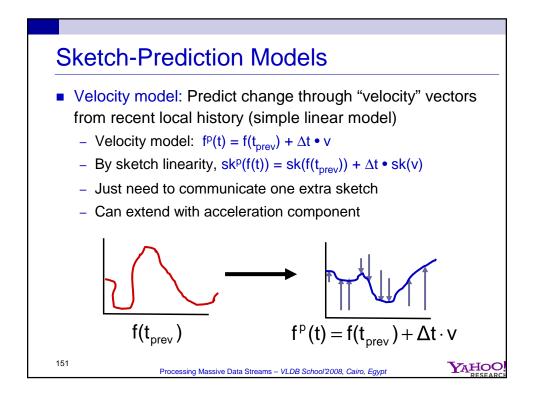




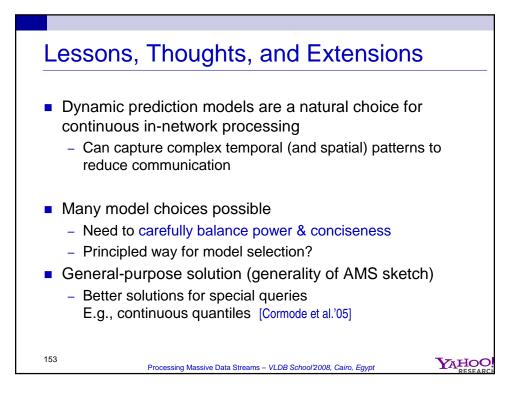


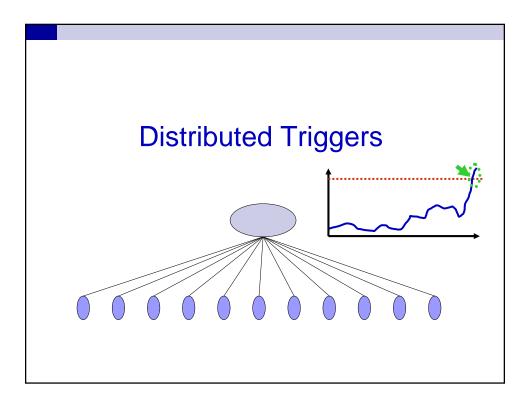


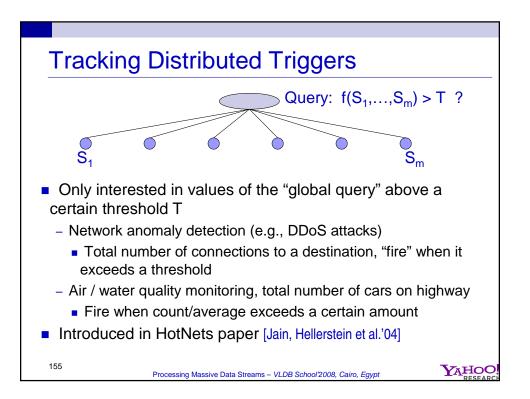


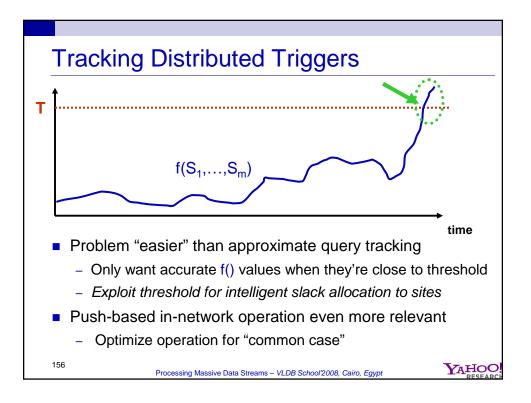


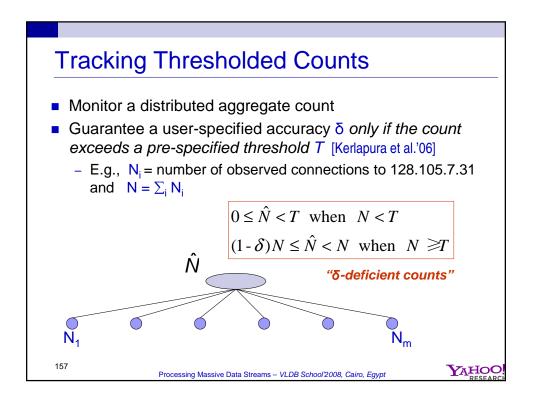
Model	Info	Predicted Sketch
Static	ø	$sk^{p}(f(t)) = sk(f(t_{prev}))$
Velocity	sk(v)	$\mathbf{sk}^{p}(\mathbf{f(t)}) = \mathbf{sk}(\mathbf{f(t_{prev})}) + \Delta t \cdot \mathbf{sk}(v)$
■ 1 – 2 orde	ers of magr	itude savings over sending all data

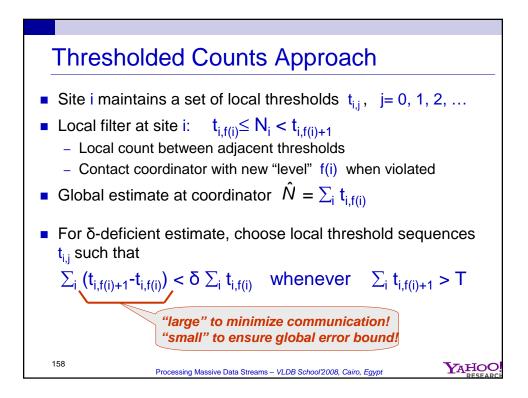


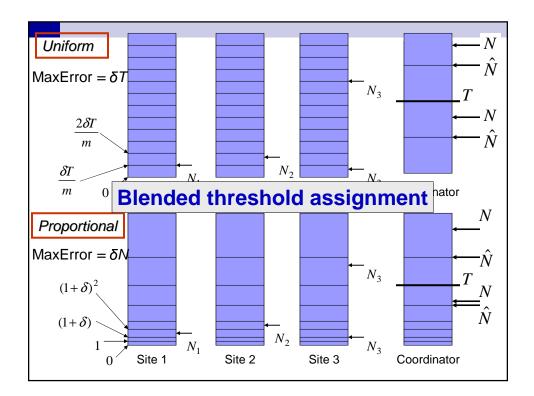


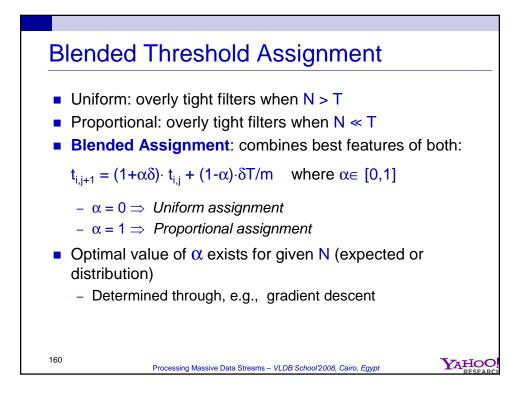


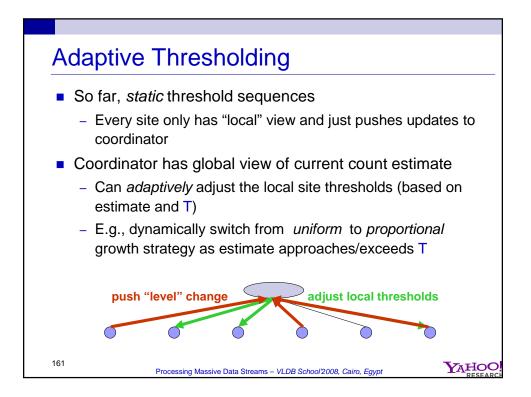


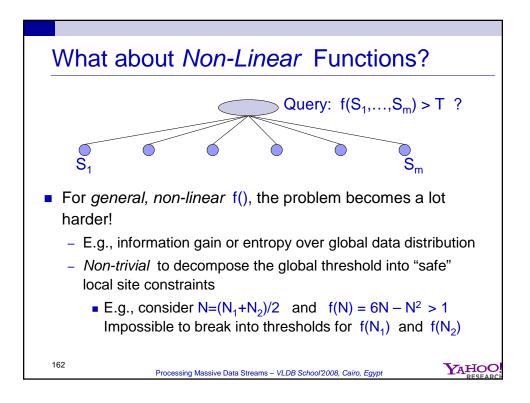


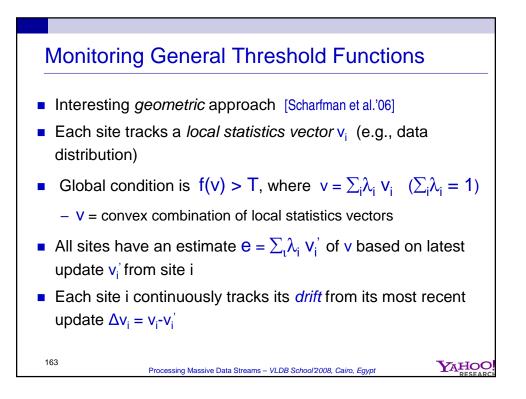


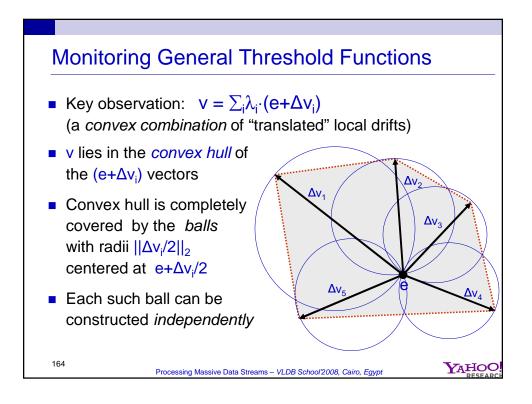


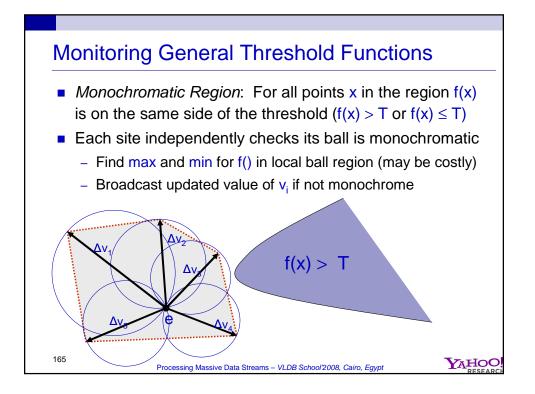


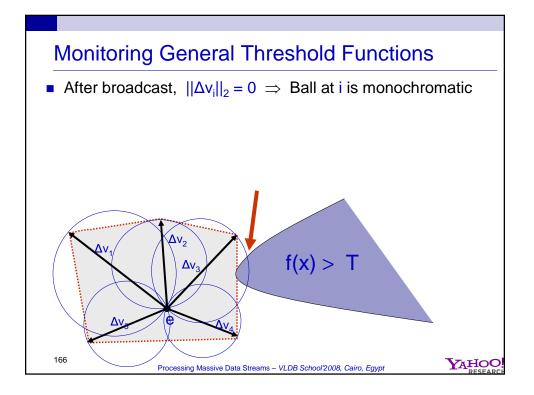


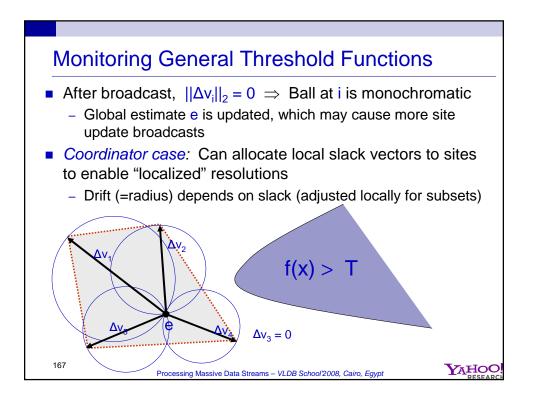


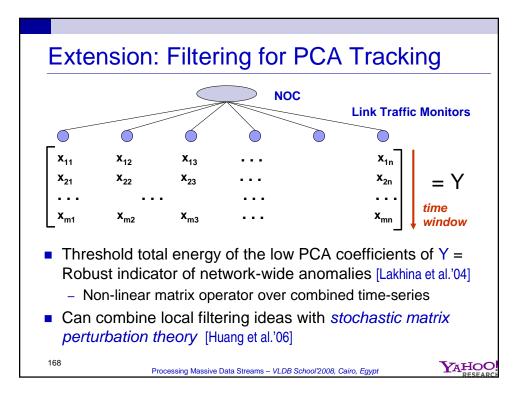


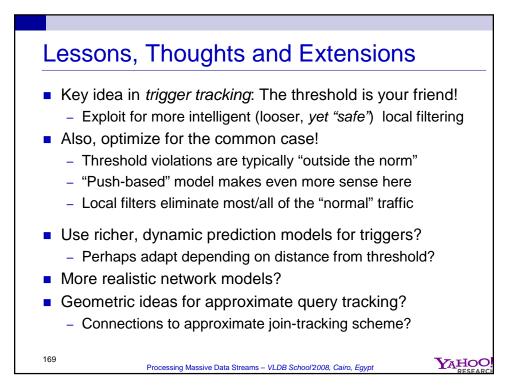


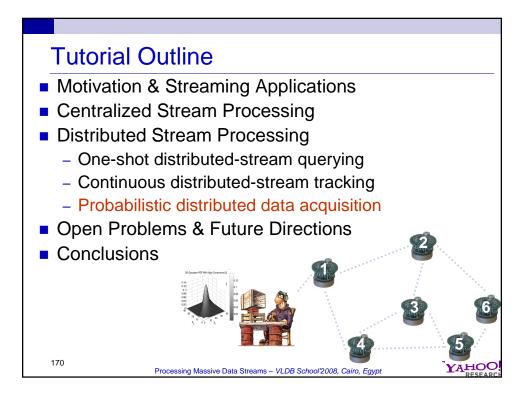


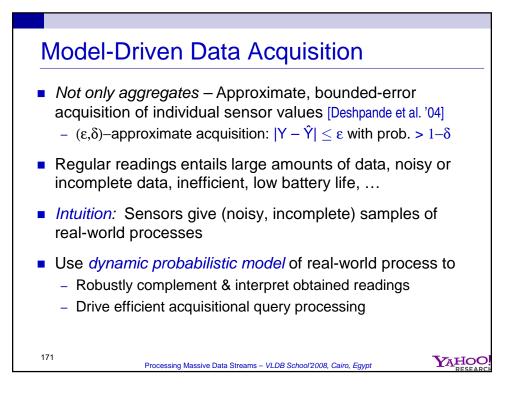


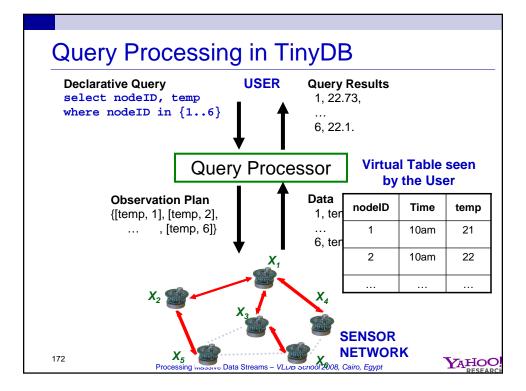


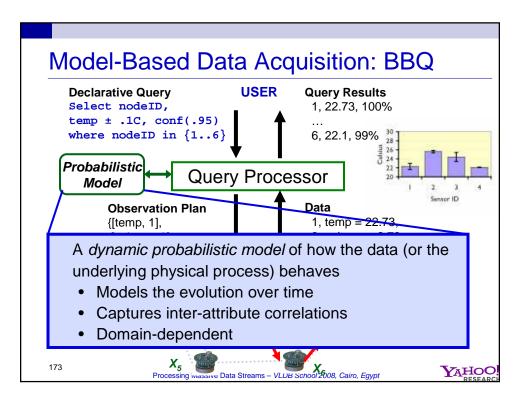


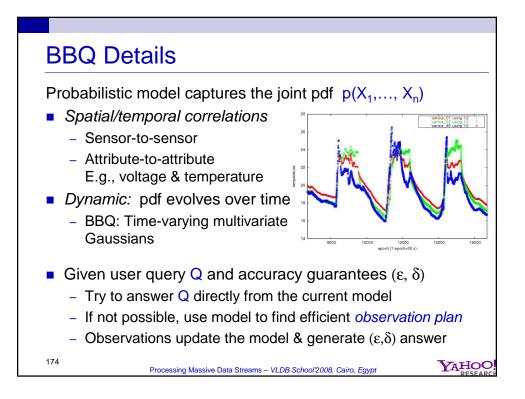


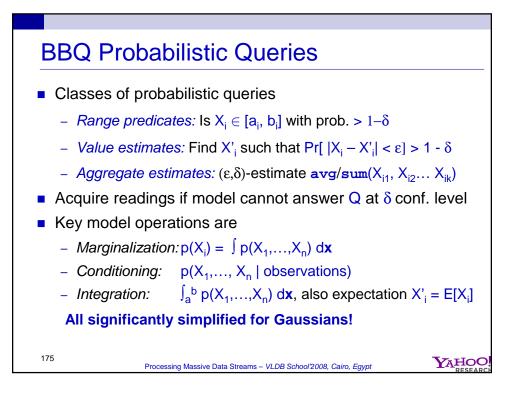


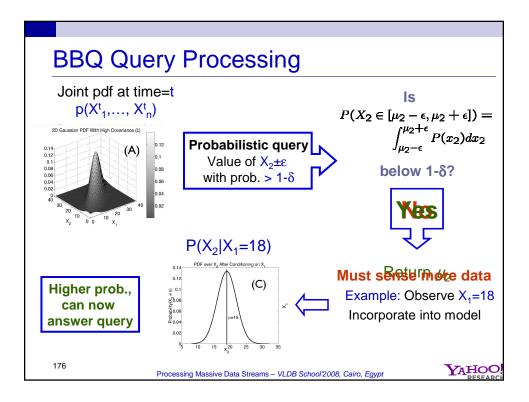


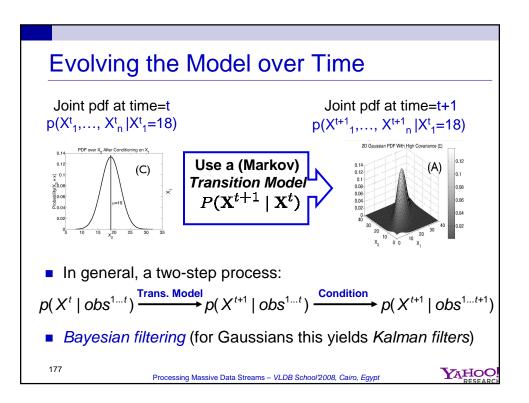


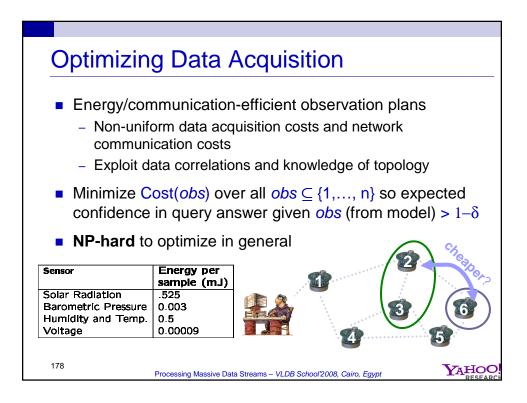


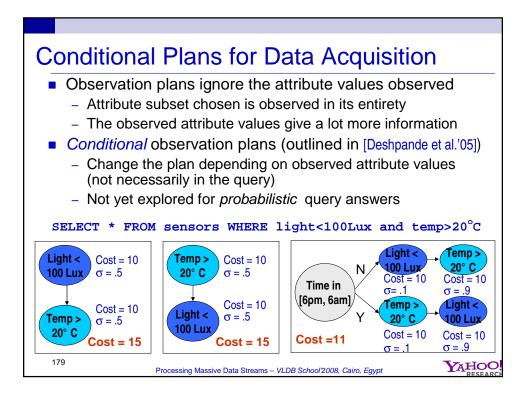


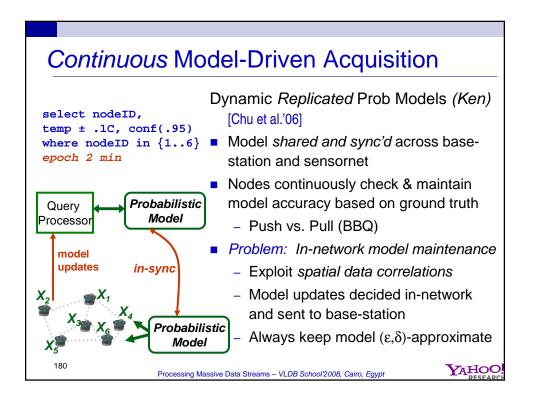


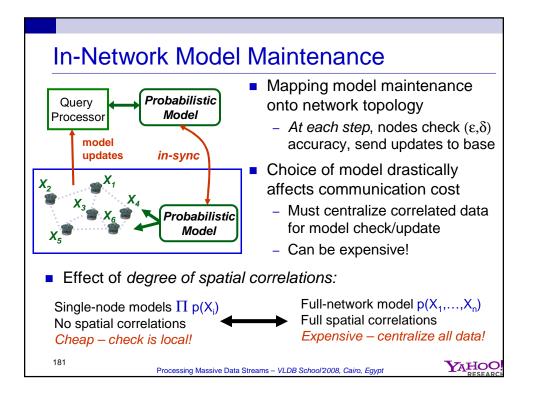


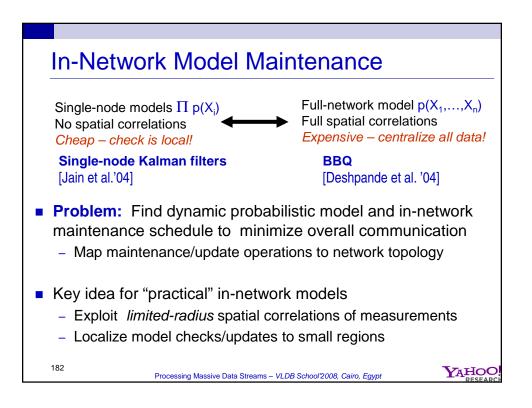


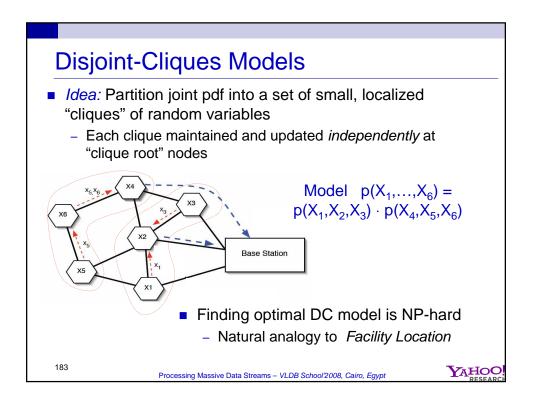


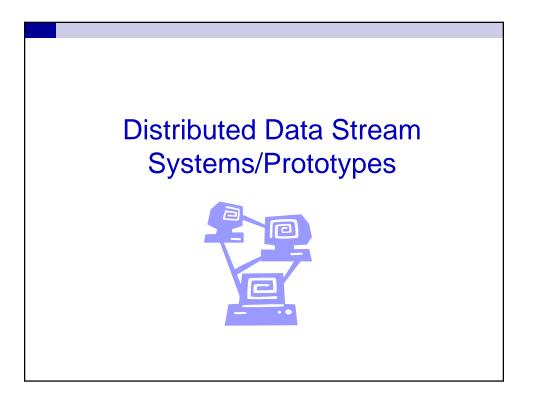


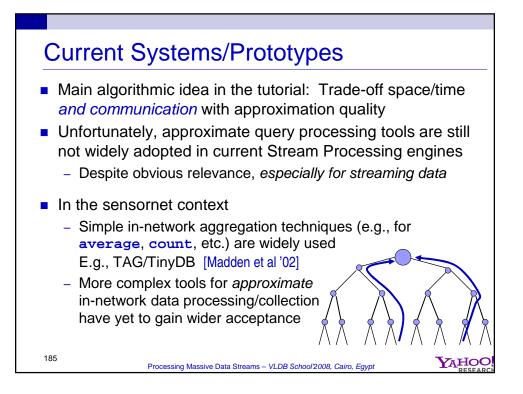


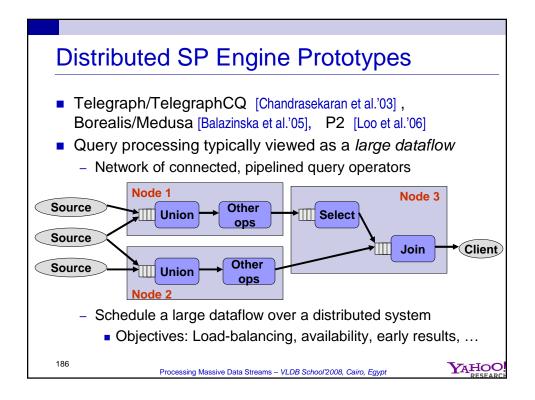


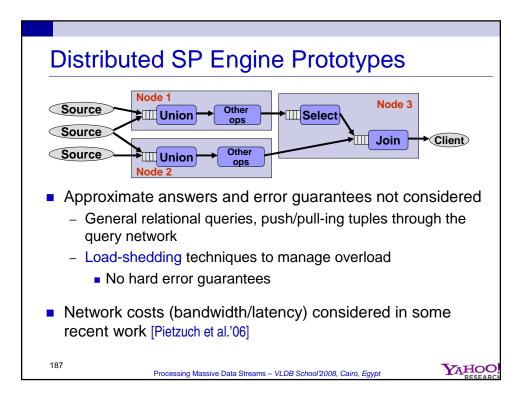


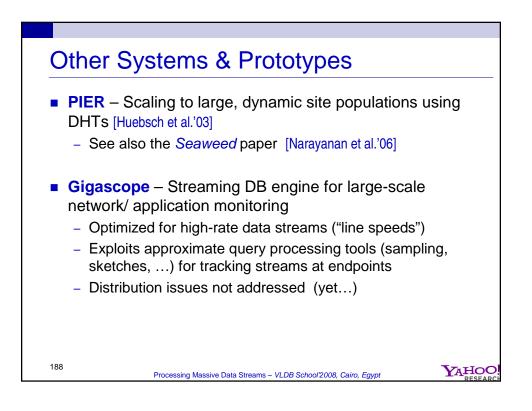


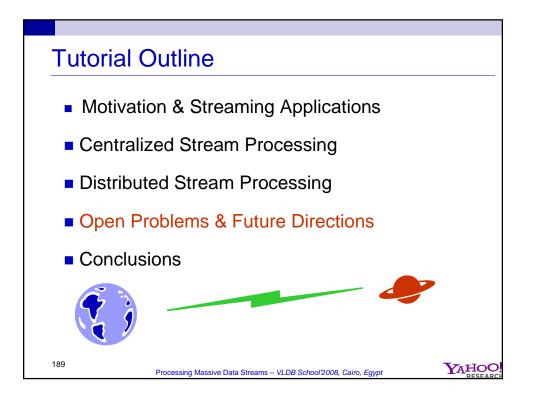


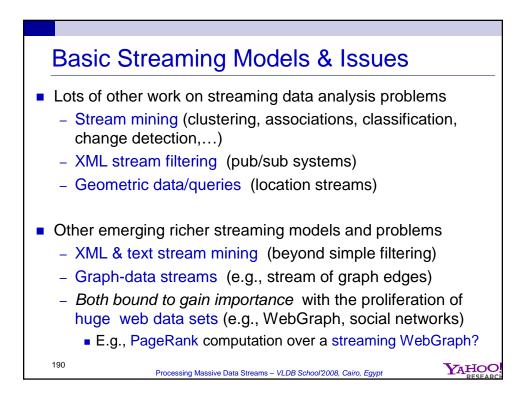


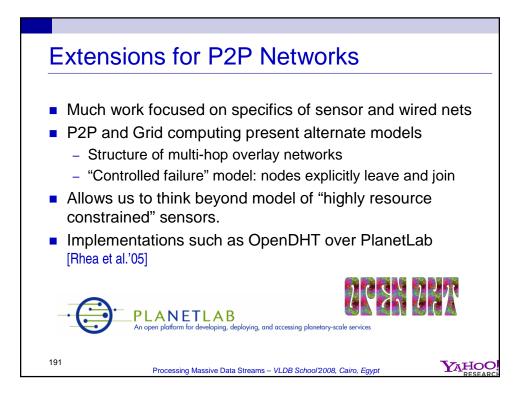


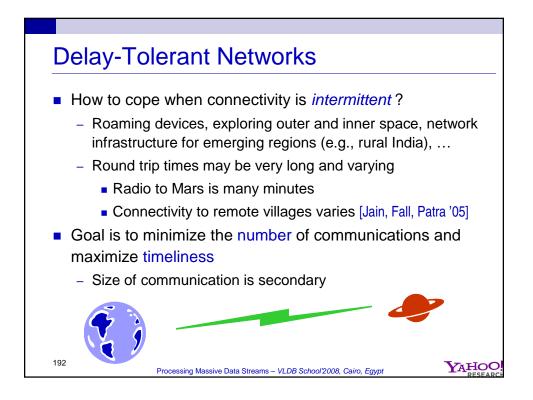


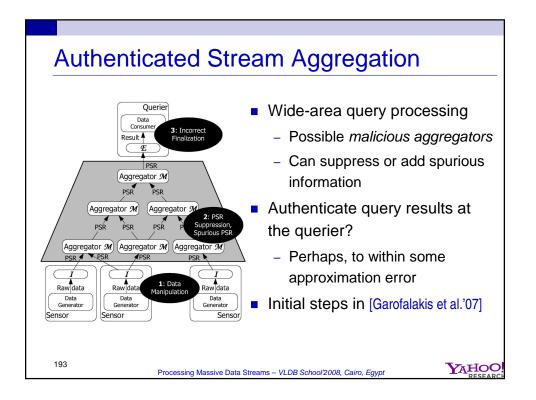


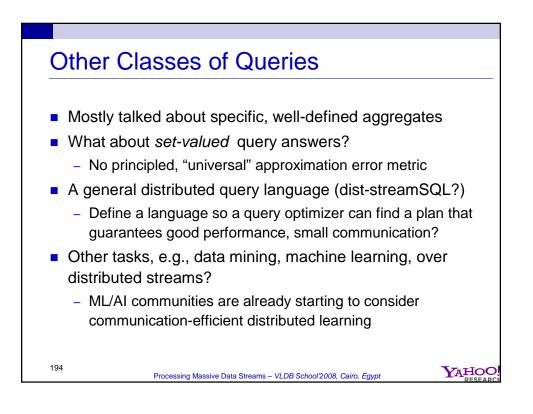


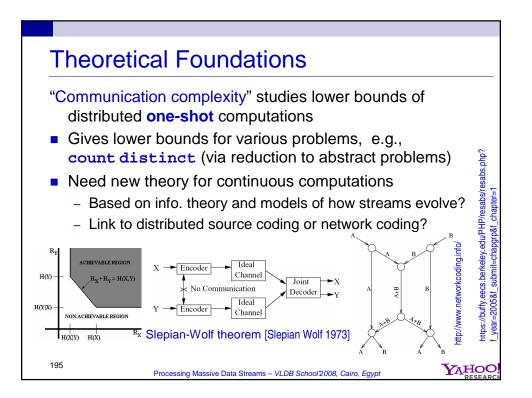


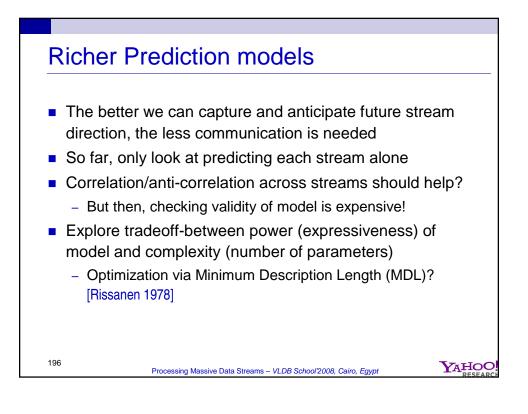


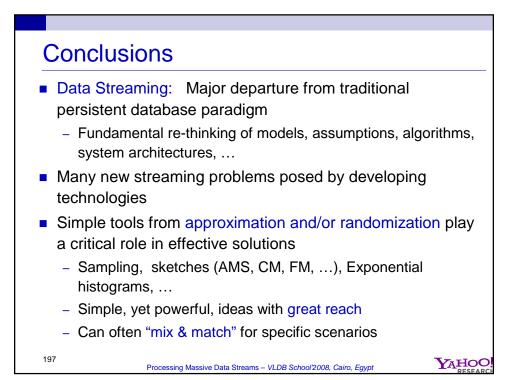


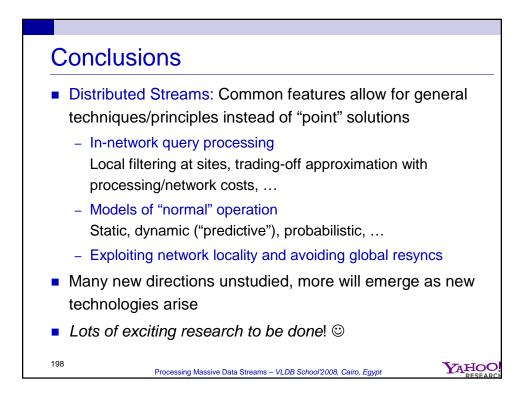
















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